

Dark Energy, Modified Gravity  
and  
The Accelerating Universe

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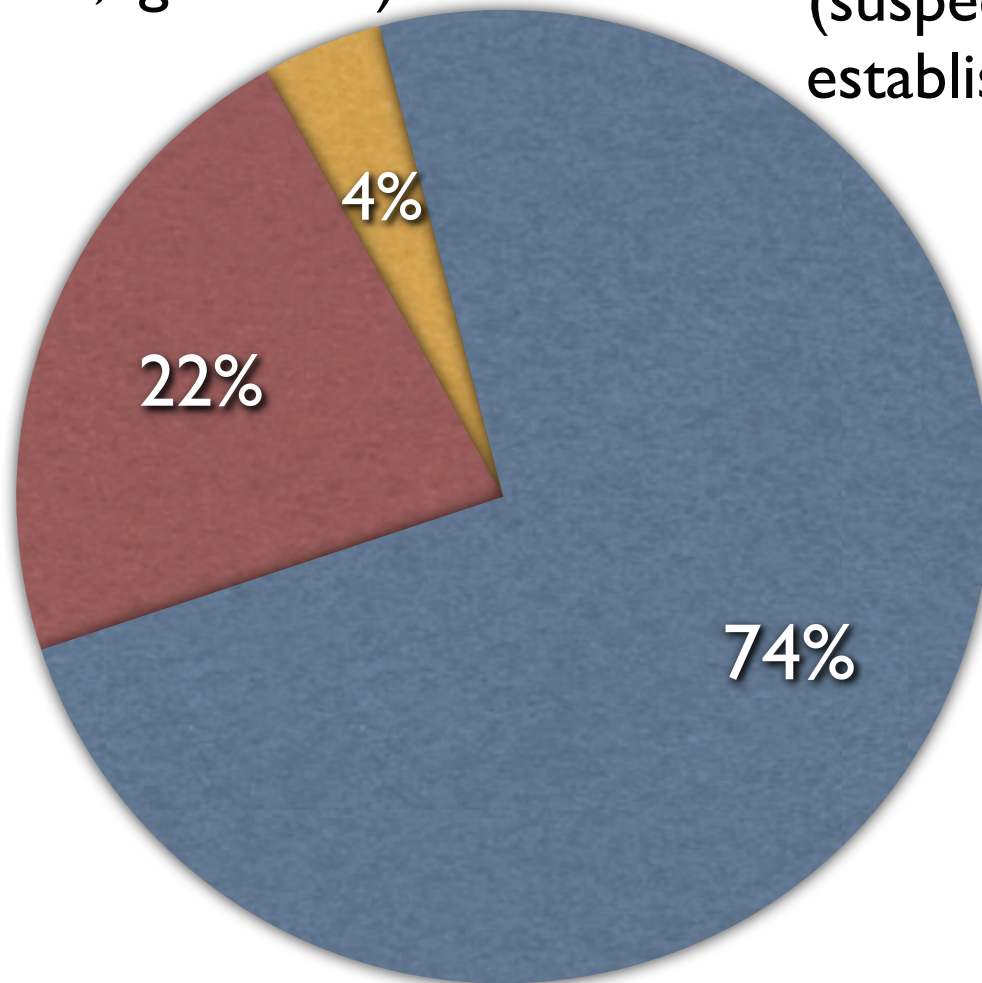
# Makeup of universe today

**Baryonic Matter**  
(stars 0.4%, gas 3.6%)

**Dark Energy**  
(suspected since 1980s  
established since 1998)

**Dark Matter**  
(suspected since 1930s  
established since 1970s)

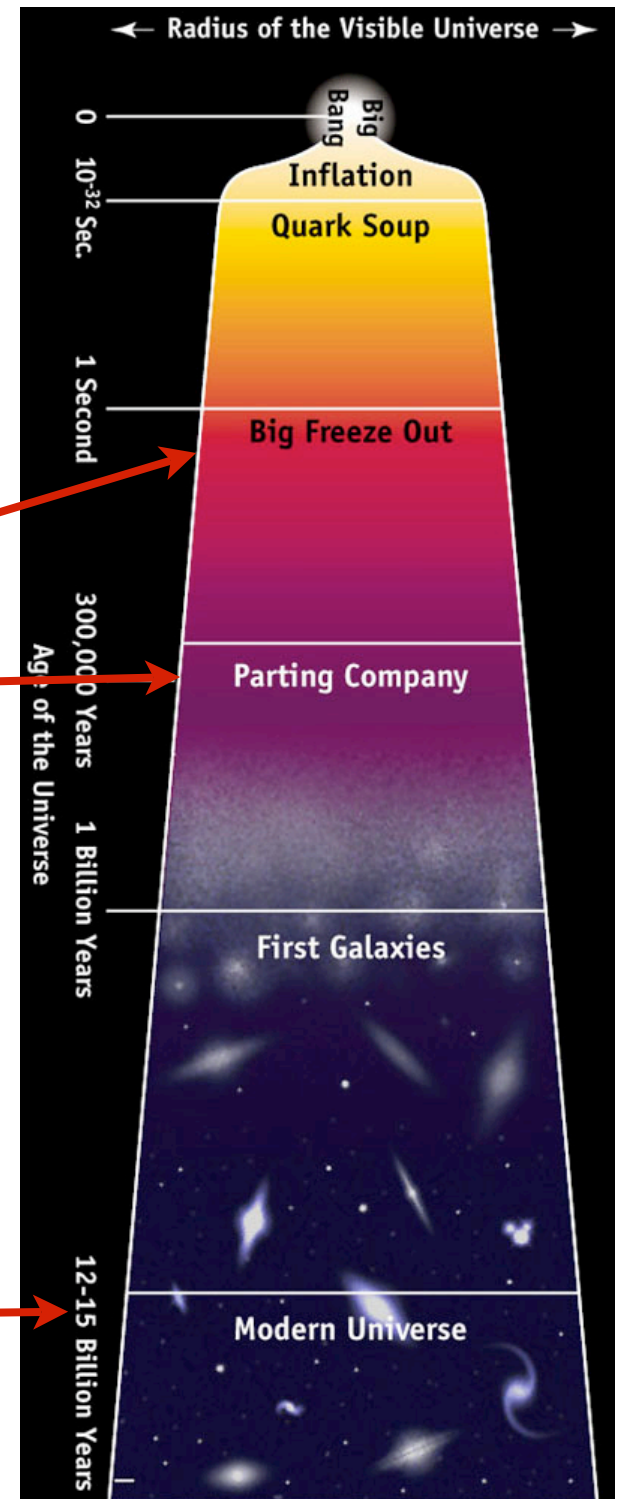
Also:  
radiation (0.01%)



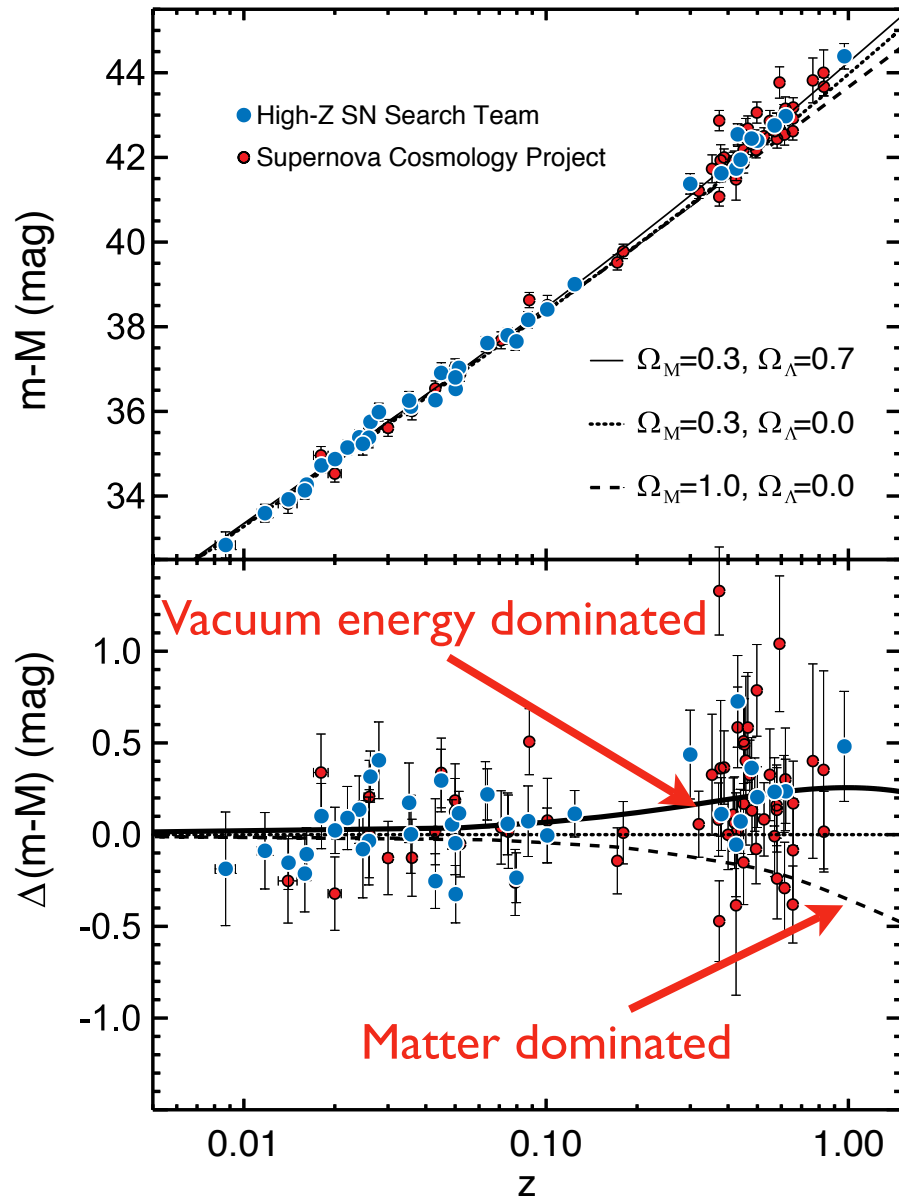
Some of the early history of the Universe is actually understood better!

Physics quite well understood

95% of contents only phenomenologically described



# DE status $\sim 8$ years after discovery



Measurements much better, LCDM still a good fit

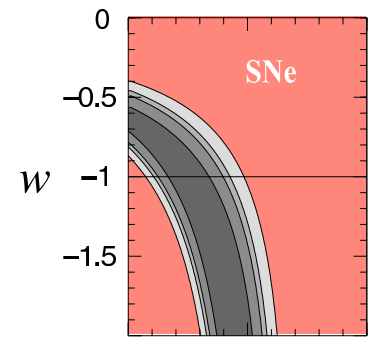
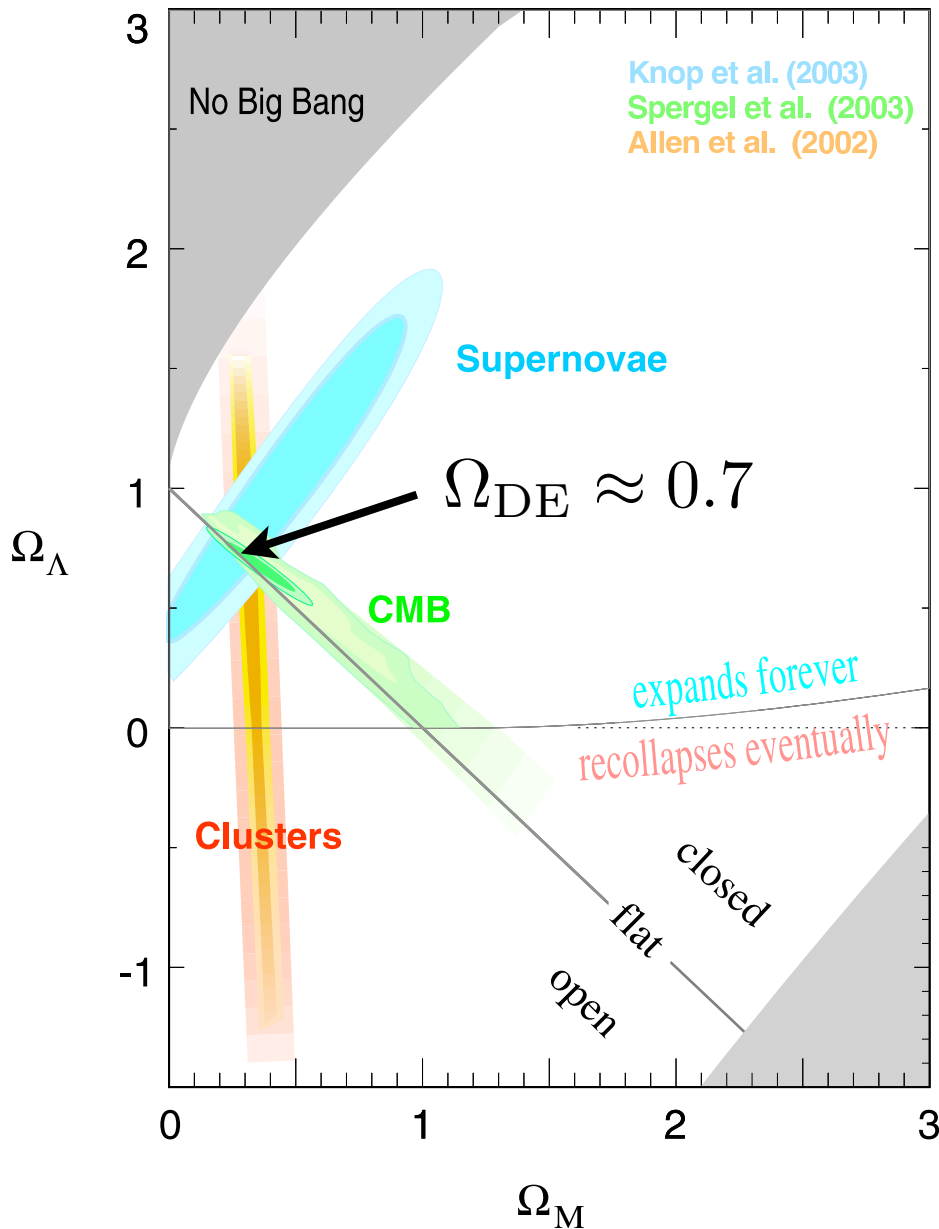
Strong indirect (non-SNa Ia) evidence for DE from CMB+LSS

Physical mechanism responsible completely unknown

A lot of work on modified gravity proposals and observational signatures

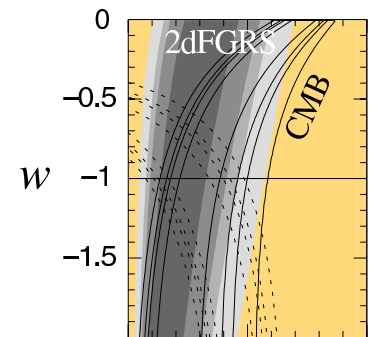
# Current constraints

Supernova Cosmology Project

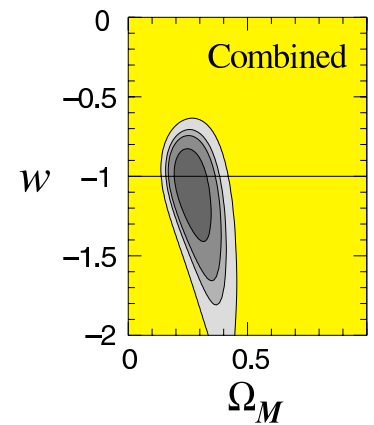


Supernova Cosmology Project  
Knop *et al.* (2003)

*Assuming constant w*



With limits from;  
2dFGRS (Hawkins *et al.* 2002)  
and CMB (Bennet *et al.* 2003,  
Spergel *et al.* 2003)



$w = -1.05^{+0.15}_{-0.20}$  (statistical)  
 $\pm 0.09$  (systematic)

# What if gravity deviates from GR?

For example:

$$H^2 - F(H) = \frac{8\pi G}{3} \rho, \quad \text{or} \quad H^2 = \frac{8\pi G}{3} \left( \rho + \frac{3F(H)}{8\pi G} \right)$$



Modified gravity



Dark energy

# Modified gravity proposals

- Introduce modifications to GR (typically near horizon scale) to explain the observed acceleration of the universe
- Make sure Solar System tests are passed (can be hard)
- Constrain the MG theory using the cosmological data
- Try to distinguish MG vs. “standard” DE (can be hard!)

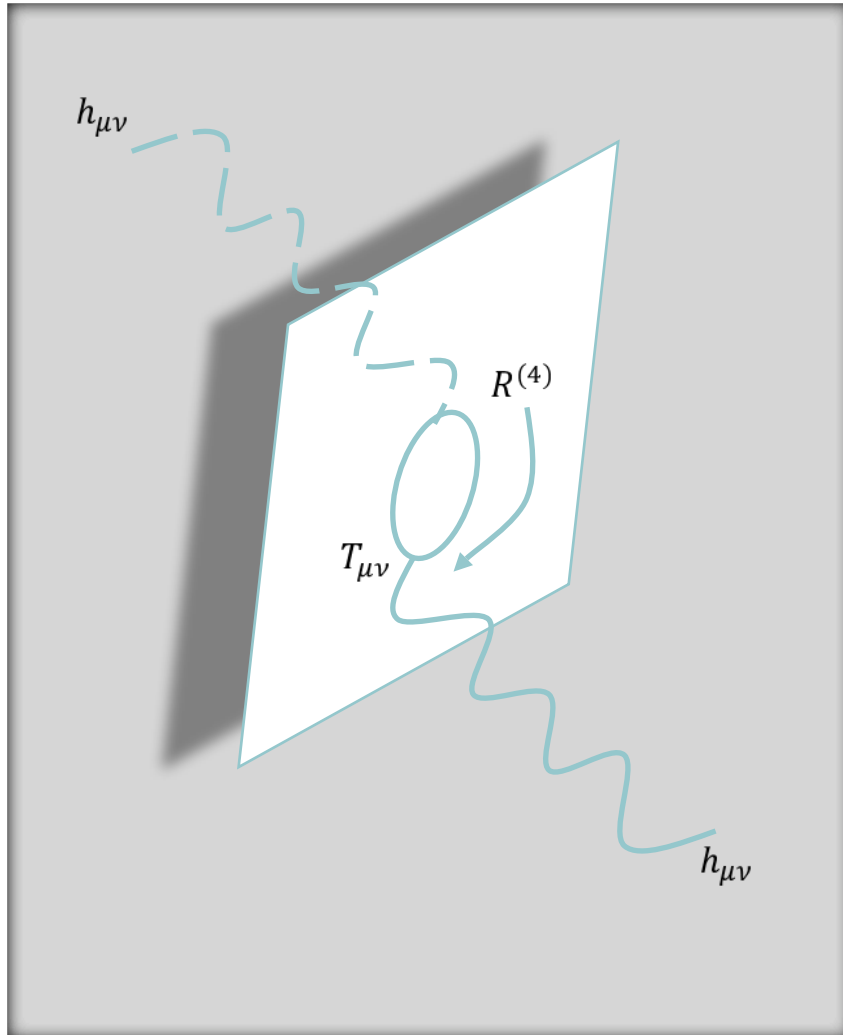
# Example: $f(R)$ gravity

$$S = \frac{1}{16\pi G} \int d^4x \sqrt{-g} [R + f(R)]$$

- Einstein equations are now 4th order
- Two classes
  - $f_{RR} < 0$  (never Matter Dominated, long range forces)
  - $f_{RR} > 0$  (MD in the past, can evade Solar system tests)



# Example: DGP braneworld theory



- 1 extra dimension (“bulk”) in which only gravity propagates
- matter lives on the “brane”
- weakening of gravity at large distances = appearance of DE

Credit: Iggy Sawicki

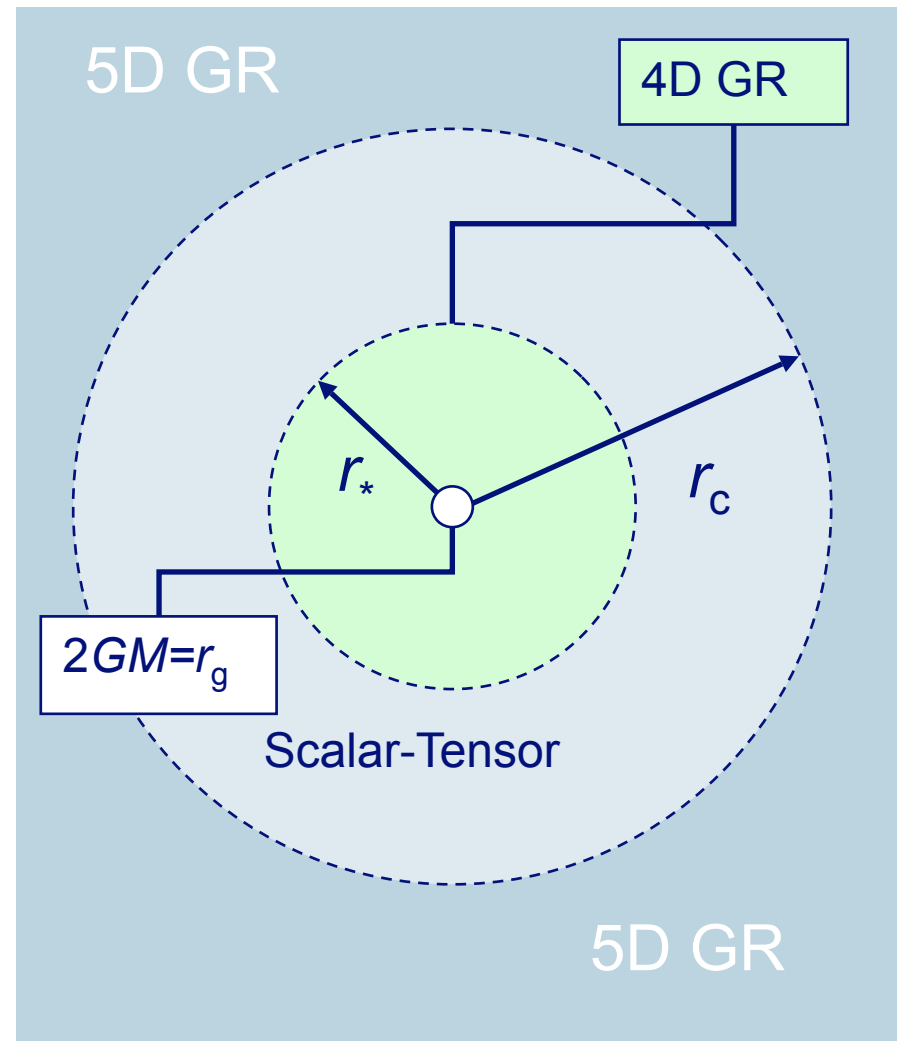
Dvali, Gabadadze & Porrati 2000; Deffayet 2001

# The structure of DGP

$$H^2 - \frac{H}{r_c} = \frac{8\pi G}{3} \rho$$

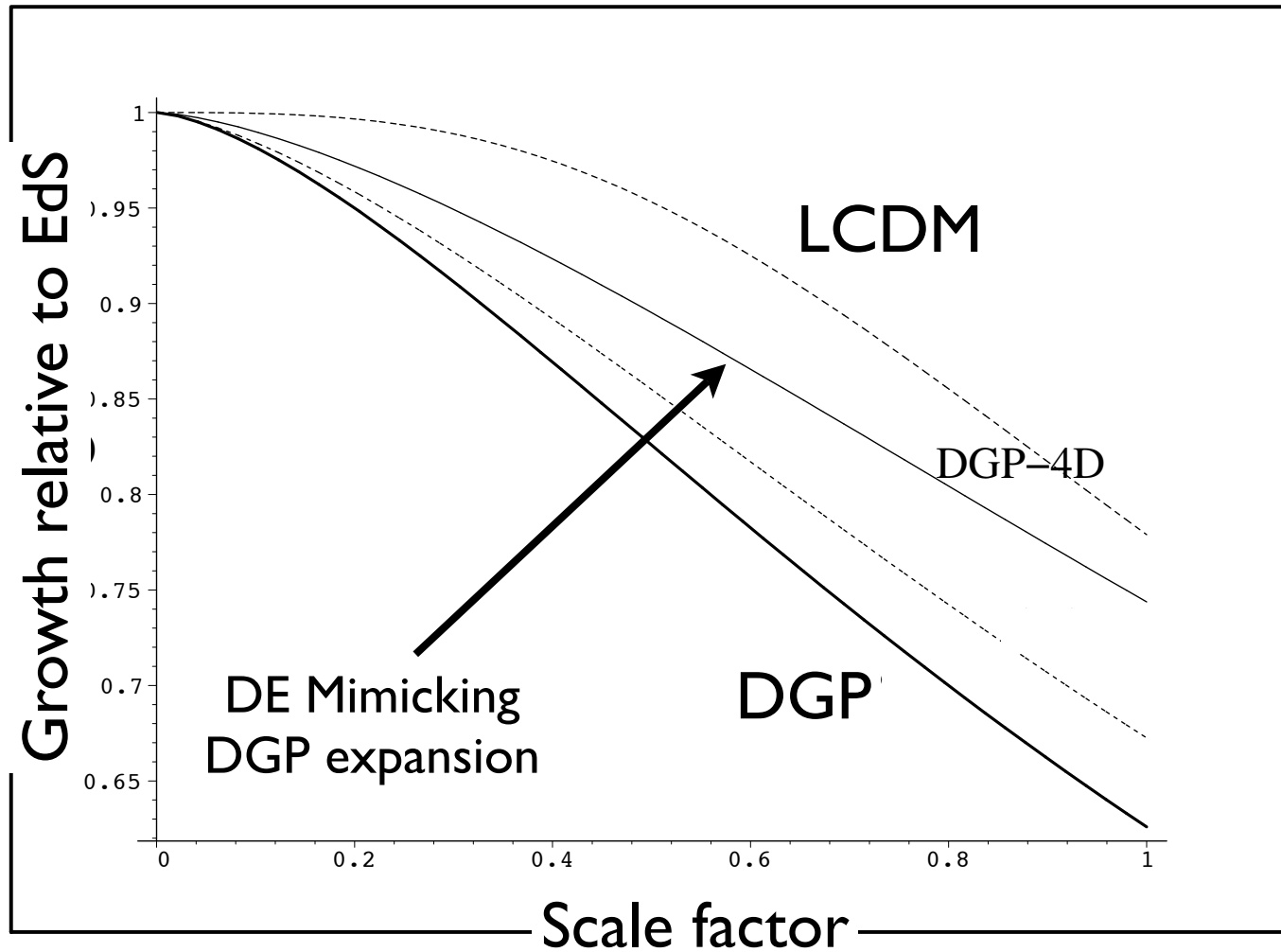
$r_c$  is a free parameter  
(to be consistent with  
observation,  $r_c \sim 1/H_0$ )

New scale  $r_* = (r_g r_c^2)^{1/3}$

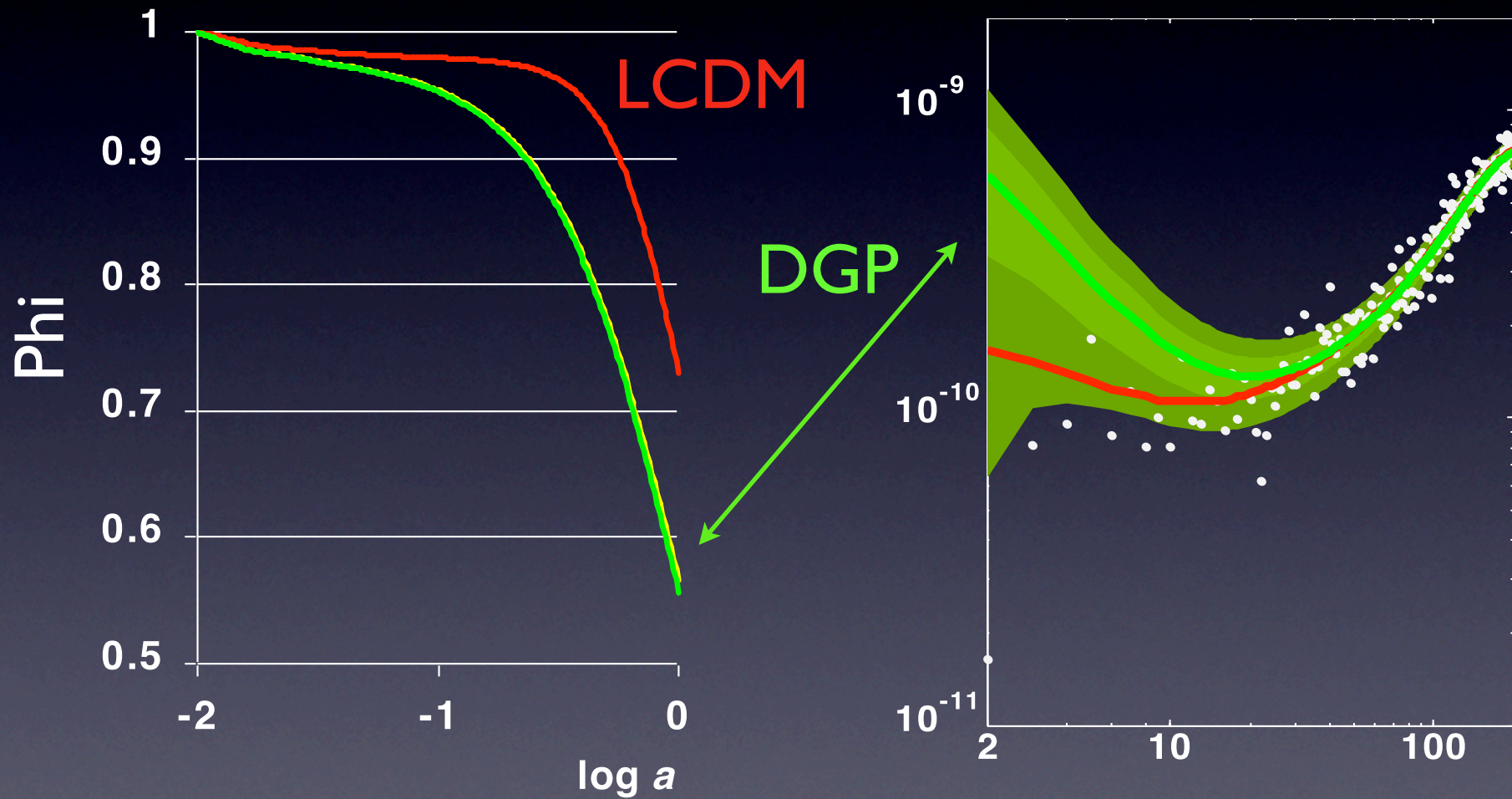


Credit: Iggy Sawicki

# DGP linear growth

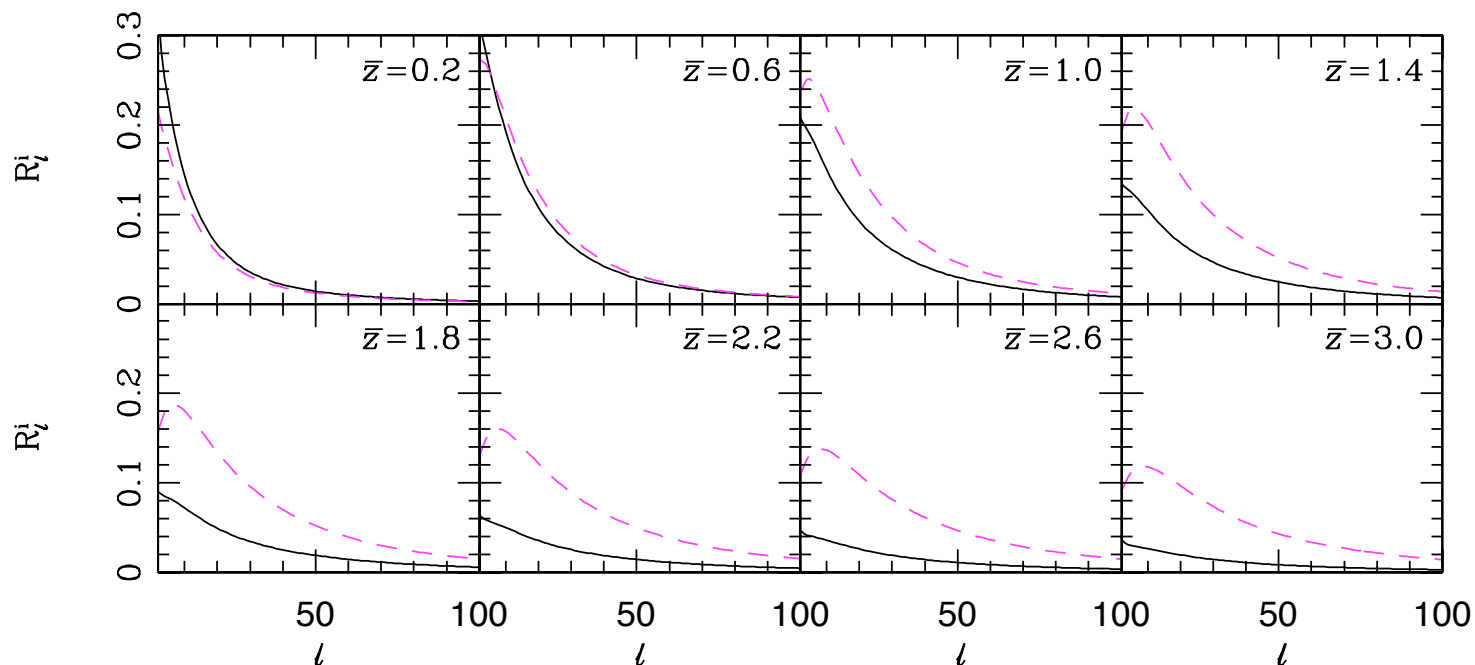


# ISW in DGP



# So DGP is (almost) ruled out

- Disfavored at a few sigma from distances (SNe etc)
- **Disfavored at a few more sigma from CMB ISW**
- Decisive rule-out will come from ISW cross-correlation at high  $z$ :



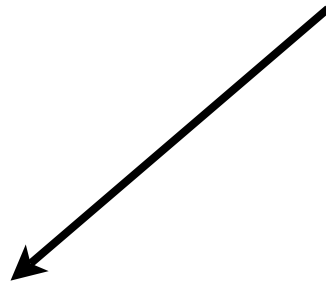
# Dark Energy or Modified Gravity?

- A given DE and modified gravity models may both fit the **expansion history** data very well
- But they will predict different **structure formation history**, i.e. deviation from  $\ddot{\delta} + 2H\dot{\delta} - 4\pi\rho_M\delta = 0$

- In standard GR,  $H(z)$  determines distances **and** growth of structure

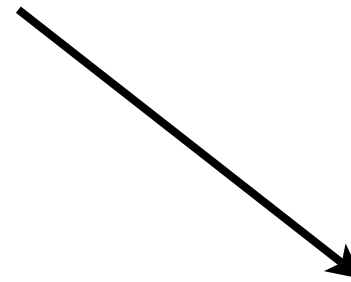
$$\ddot{\delta} + 2H\dot{\delta} - 4\pi\rho_M\delta = 0$$

- So check if this is true by measuring separately



**Distances**

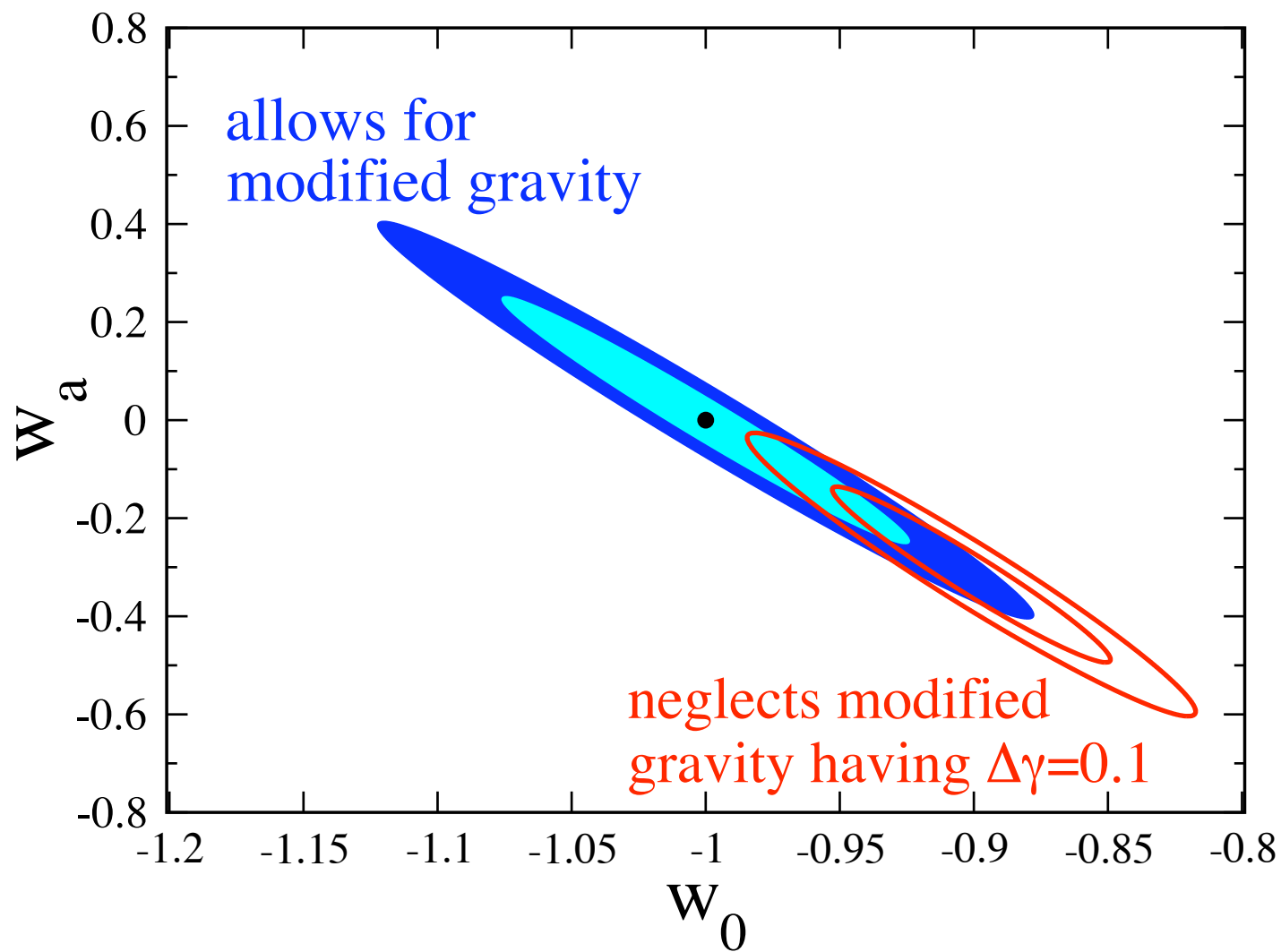
(a.k.a. kinematic probes)  
(a.k.a. 0<sup>th</sup> order cosmology)



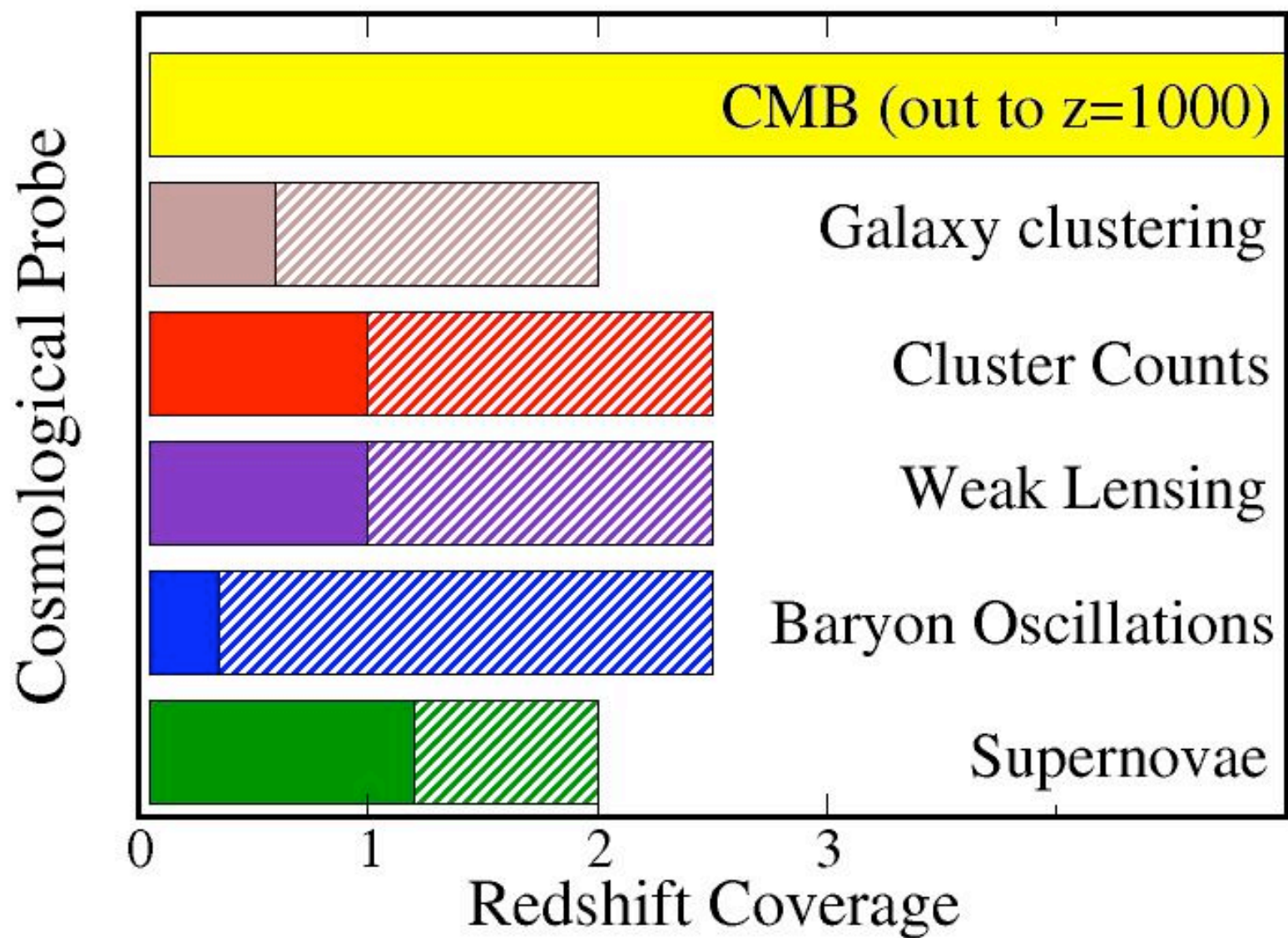
**Growth**

(a.k.a. dynamical probes)  
(a.k.a. 1<sup>st</sup> order cosmology)

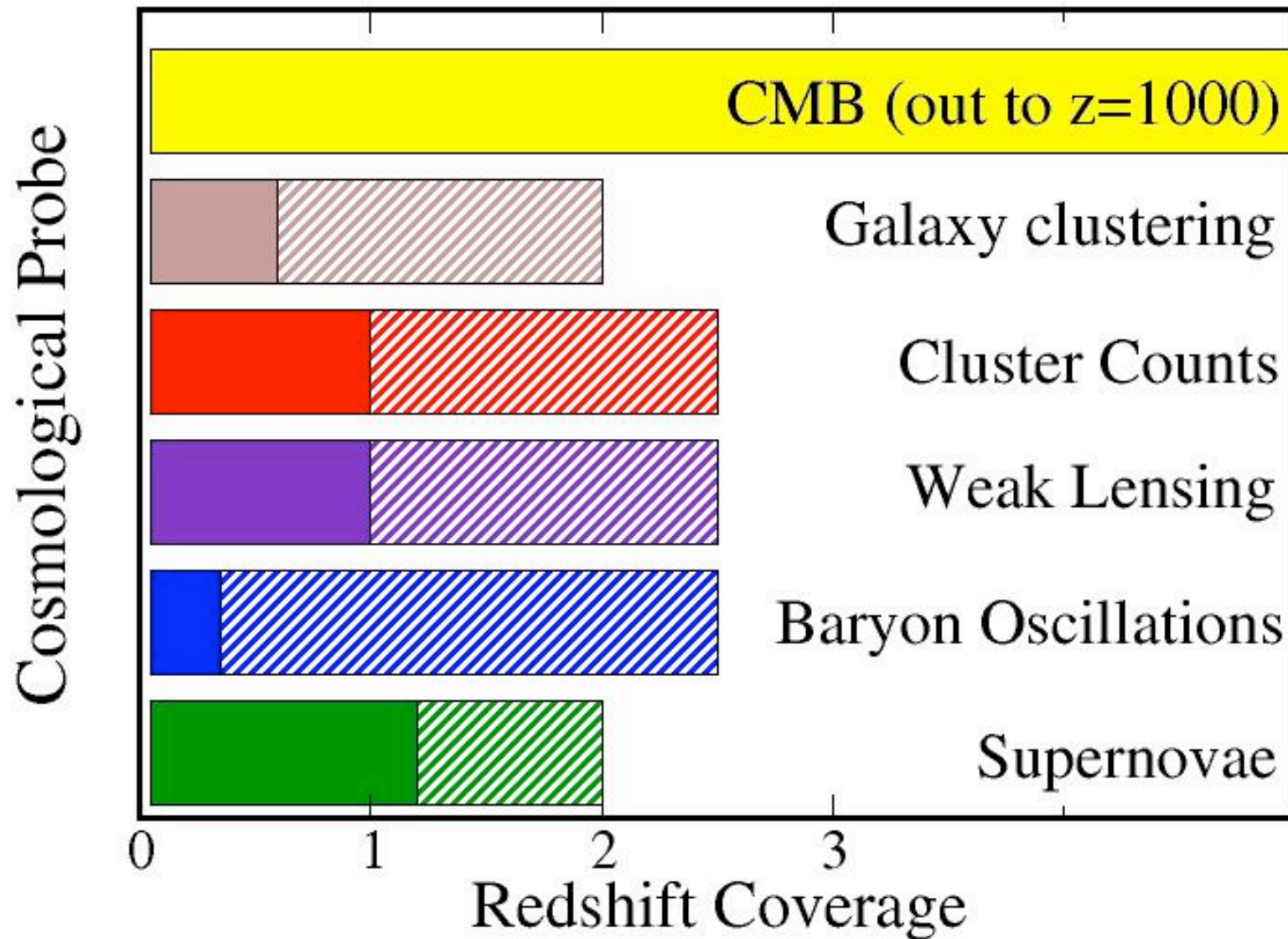
# Price of ignorance of MG







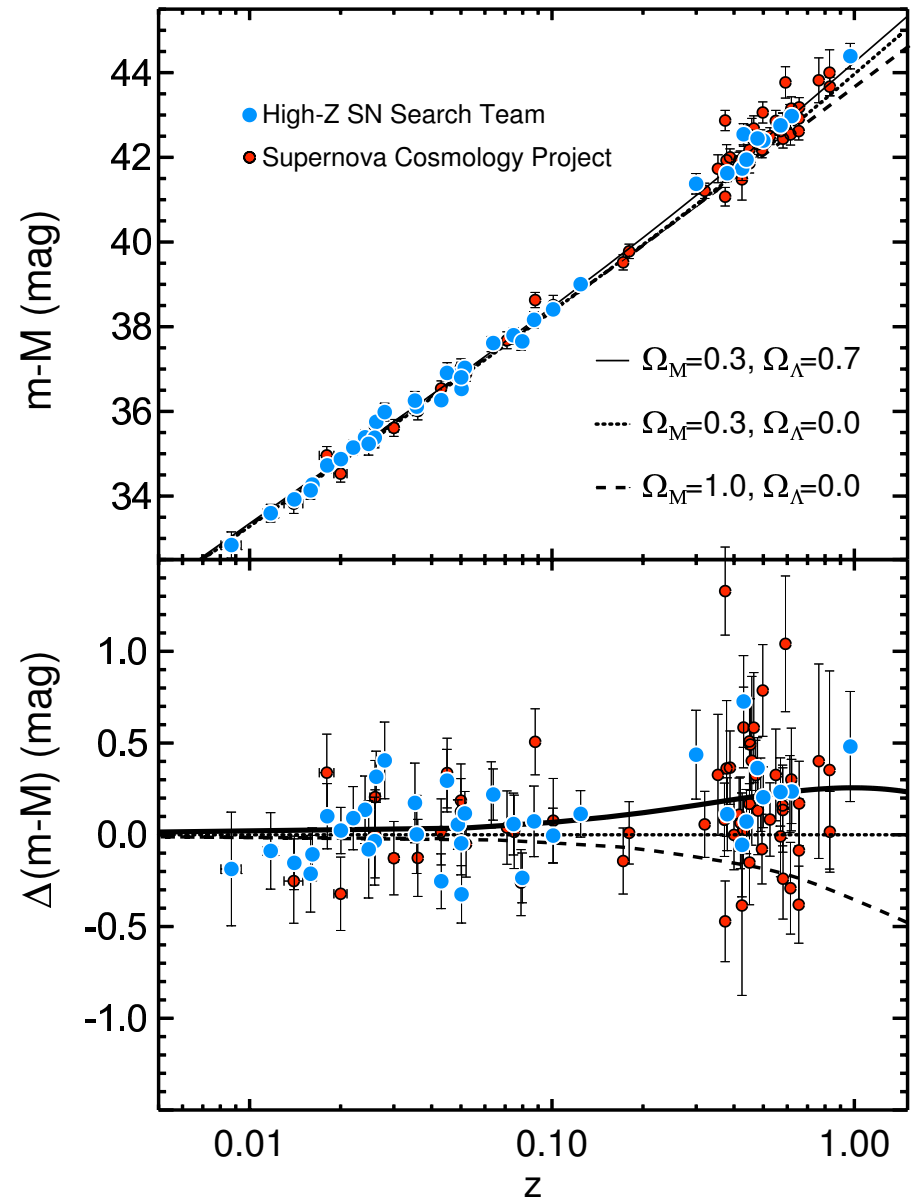
# Cosmological Probes of Dark Energy (and Modified Gravity)



# Kinematic probes: SNe Ia



- Get pure (luminosity) distances

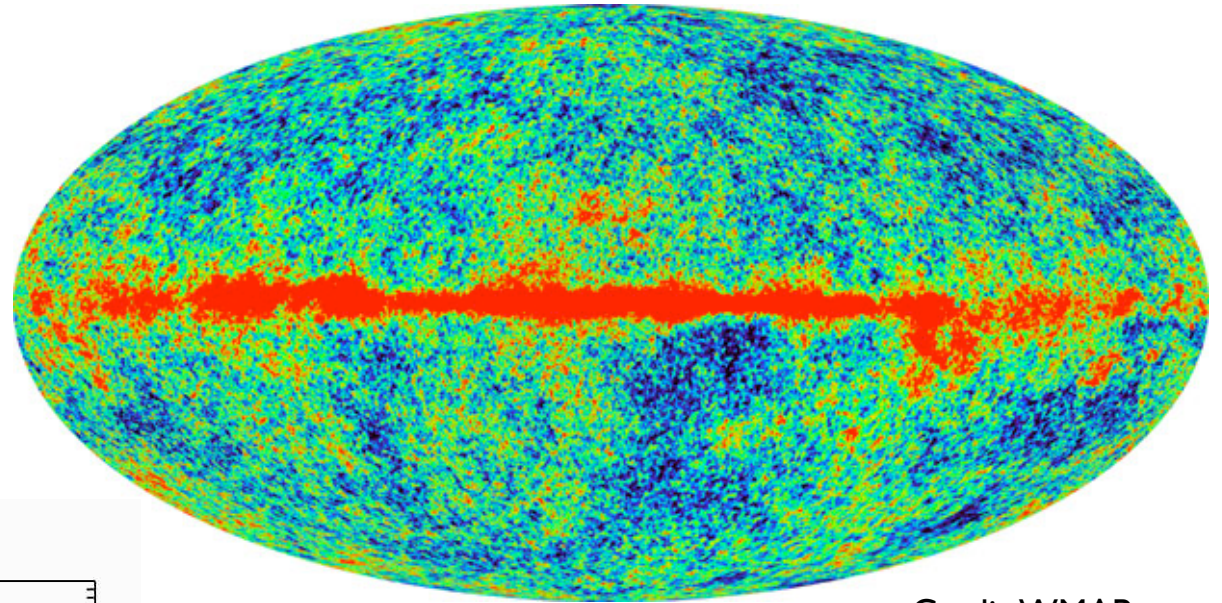




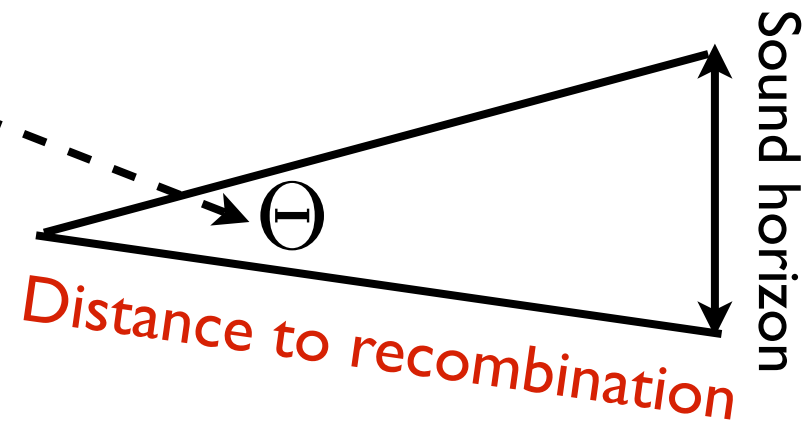
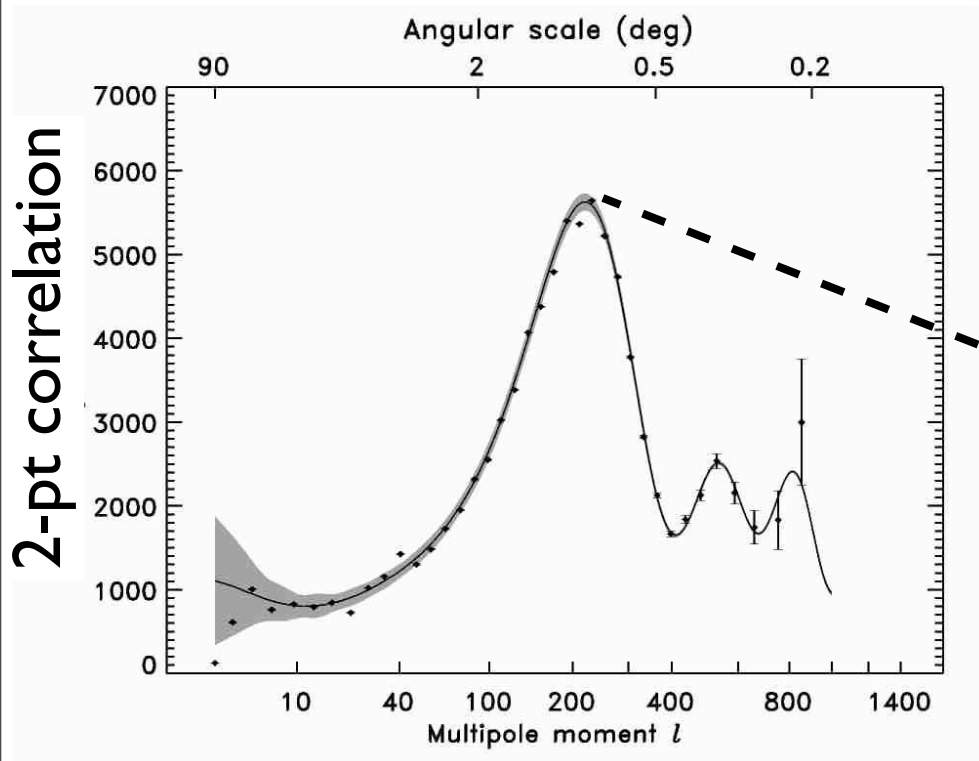
# Kinematic probes: CMB and BAO

$$T = 2.726 \text{ K}$$

$$\frac{\delta T}{T} \approx 10^{-5}$$



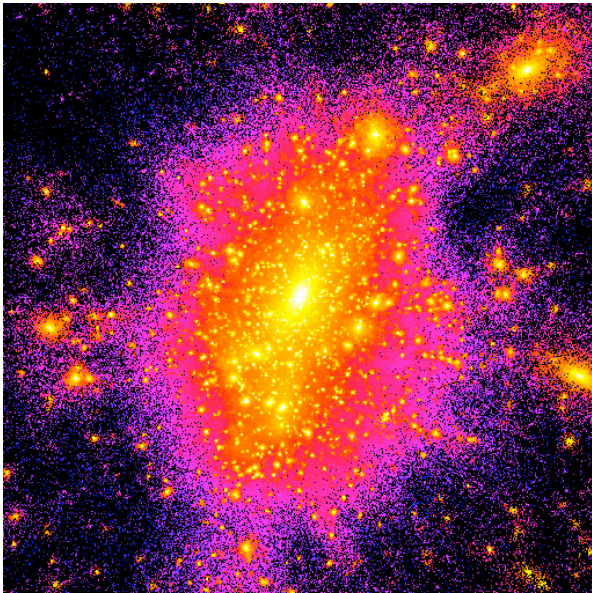
Credit: WMAP team



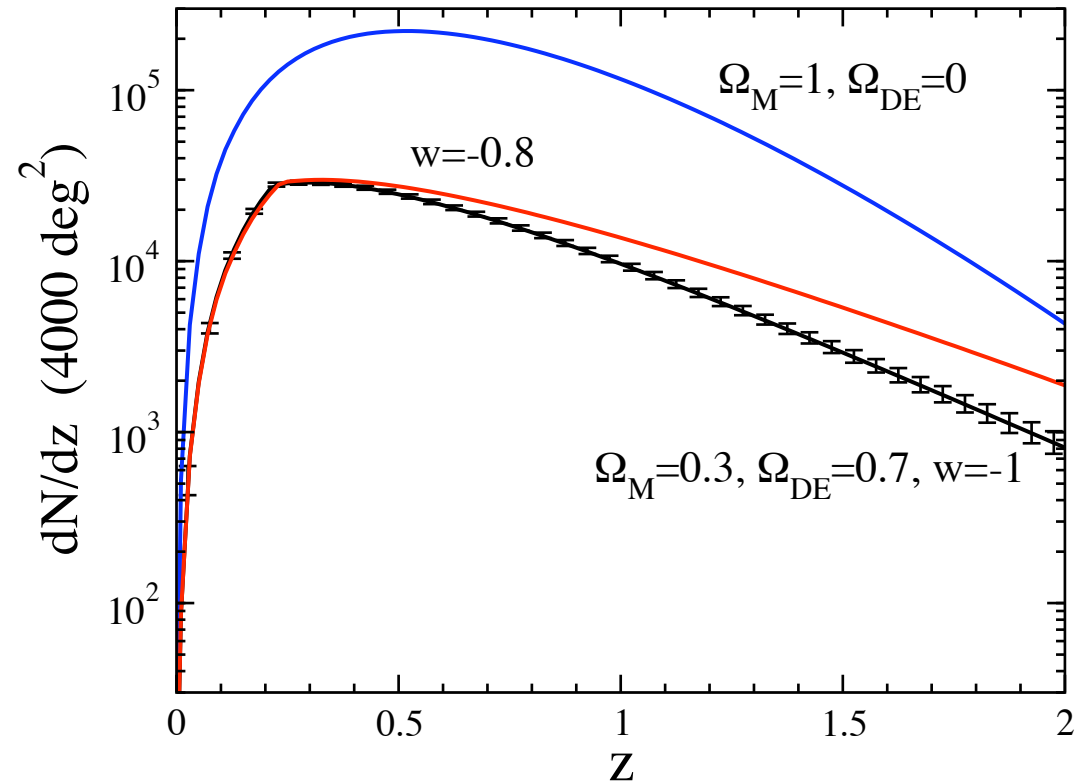
Bennett et al 2003 (WMAP collaboration)

# Structure formation probes: Galaxy cluster counts

$$\frac{d^2 N}{d\Omega dz} = n(z) \frac{r(z)^2}{H(z)}$$



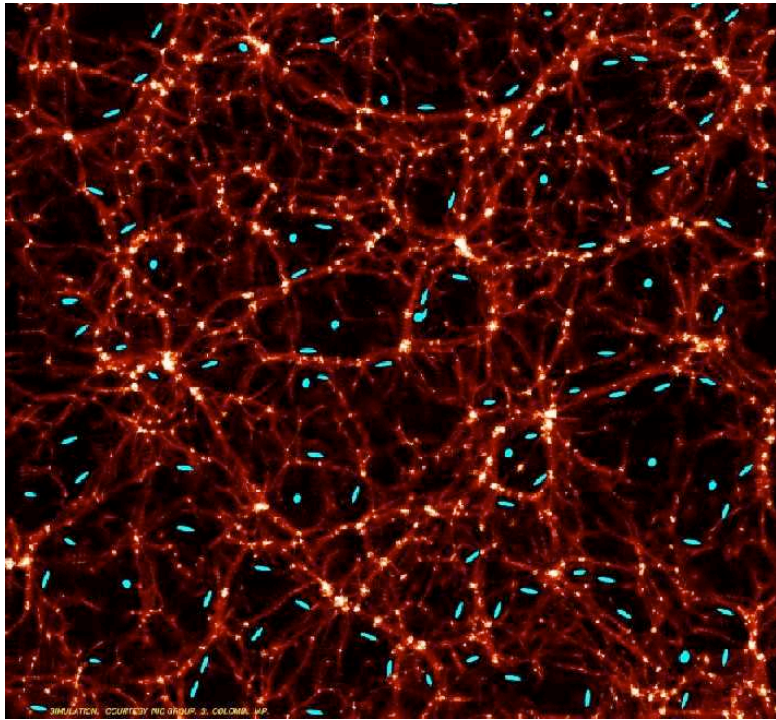
Credit: Quinn, Barnes, Babul, Gibson



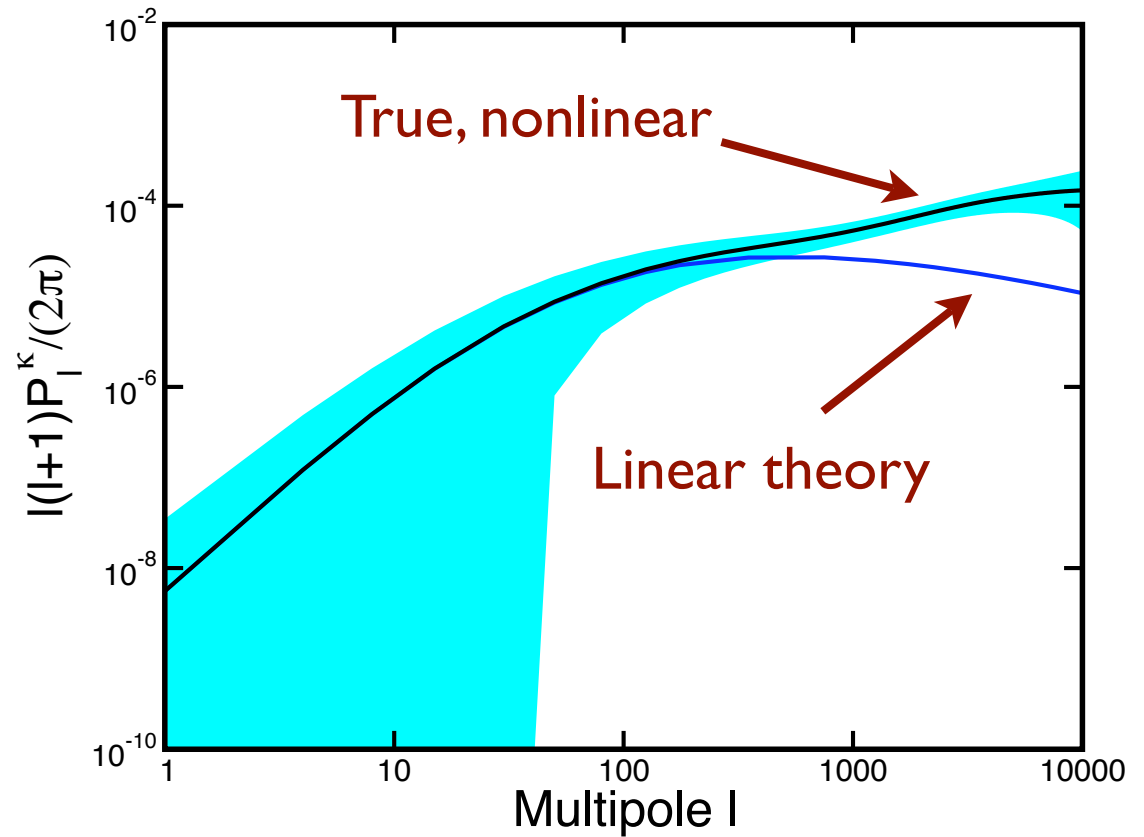
- Essentially **fully in the nonlinear regime** (scales  $\sim 1$  Mpc)

# Structure formation probes: Weak Gravitational Lensing

$$P_{\text{shear}} \simeq \int_0^\infty W(r) P_{\text{matter}}(r) dr$$



Credit: Colombi & Mellier

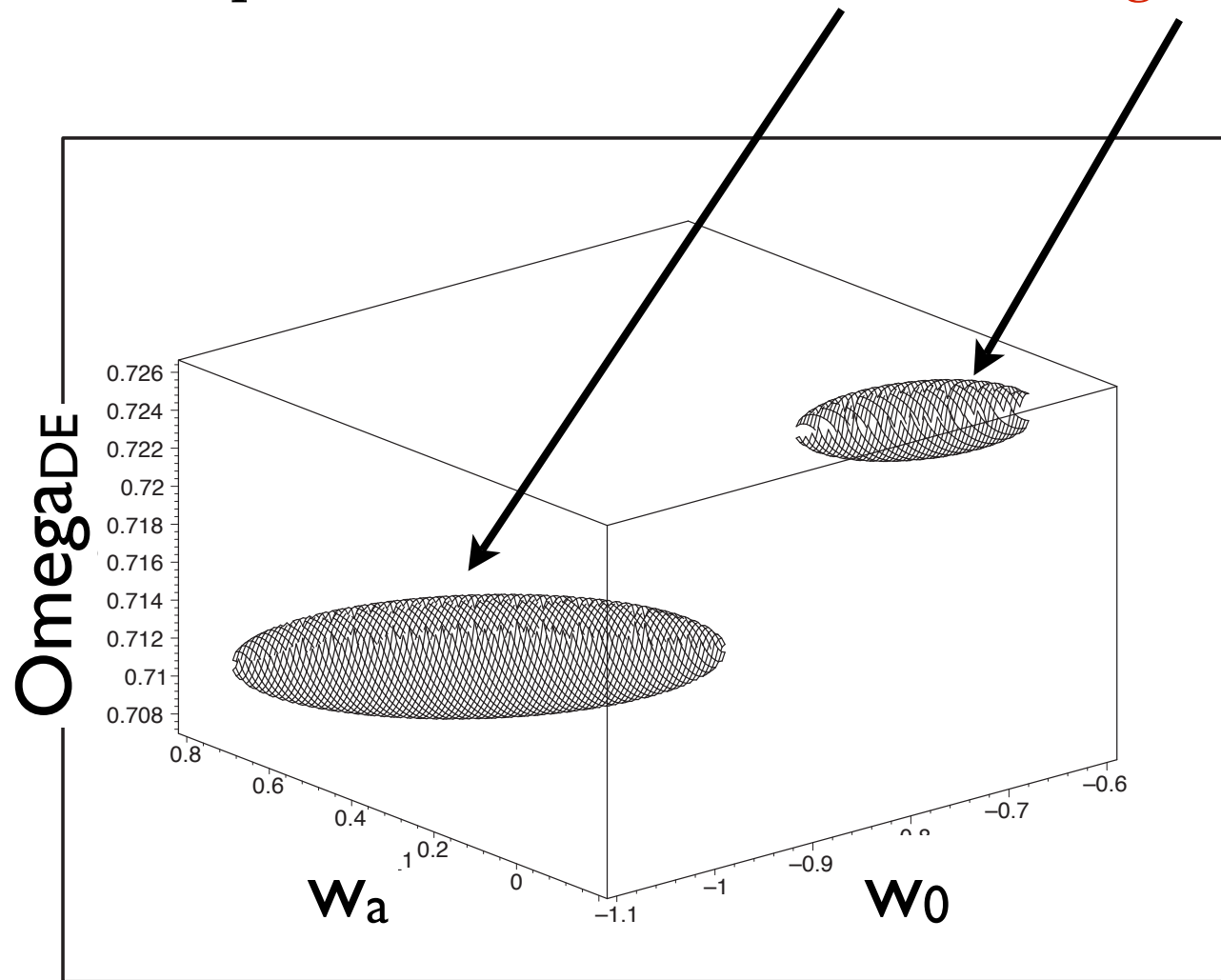


- Mostly **in the nonlinear regime** (scales  $\sim 10$  arcmin, or  $\sim 1$  Mpc)



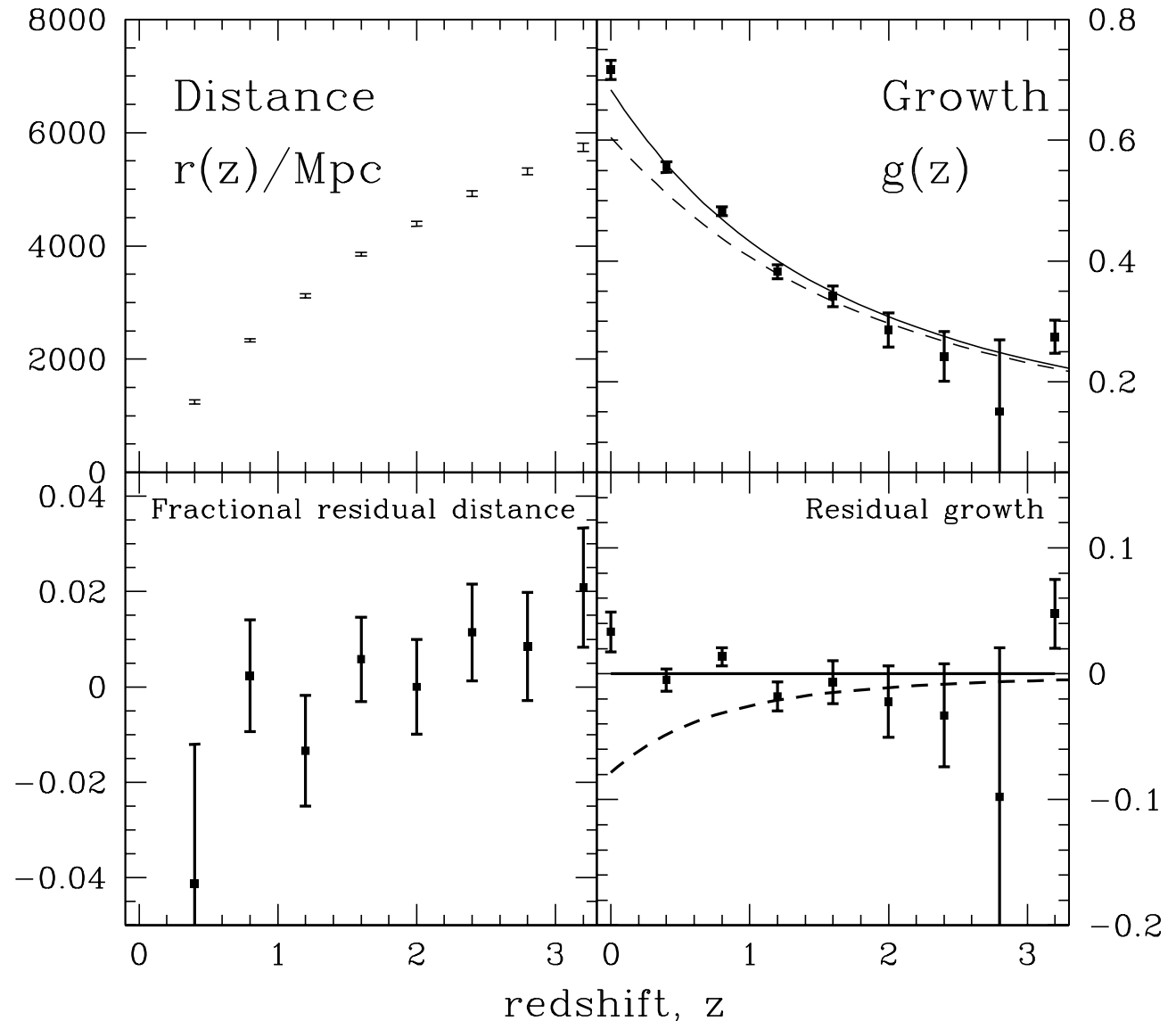
# More general approach

Measure the DE parameters from **distances** and **growth** separately



Ishak, Upadhye and Spergel 2006; others...


# Still more general approach: measure functions $r(z)$ and $g(z)$ see if they are consistent





# Minimalist Modified Gravity vs. DE

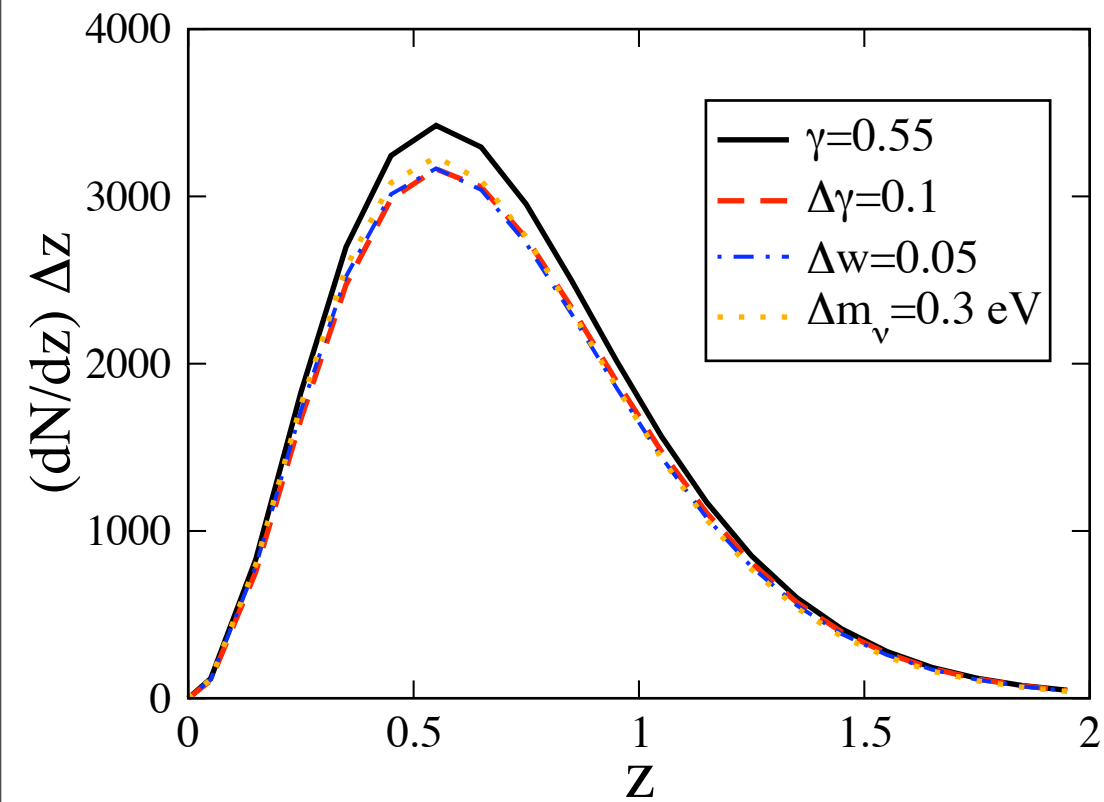
Describe deviations from GR via a **single** new parameter

$$g(a) \equiv \frac{\delta}{a} = \exp \left[ \int_0^a d \ln a [\Omega_M(a)^\gamma - 1] \right]$$


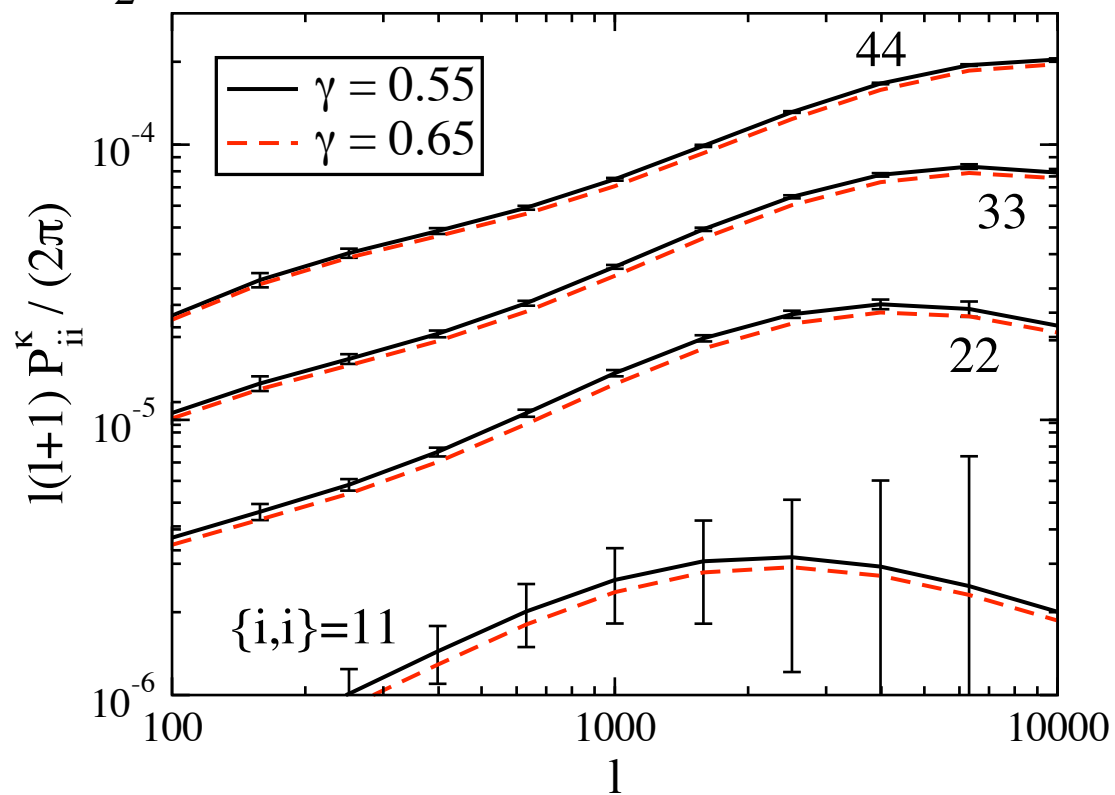
Excellent **fit** to standard DE growth function with

$$\gamma = 0.55 + 0.05[1 + w(z = 1)]$$

Also fits the DGP braneworld theory with  $\Delta\gamma = 0.13$



## Cluster counts

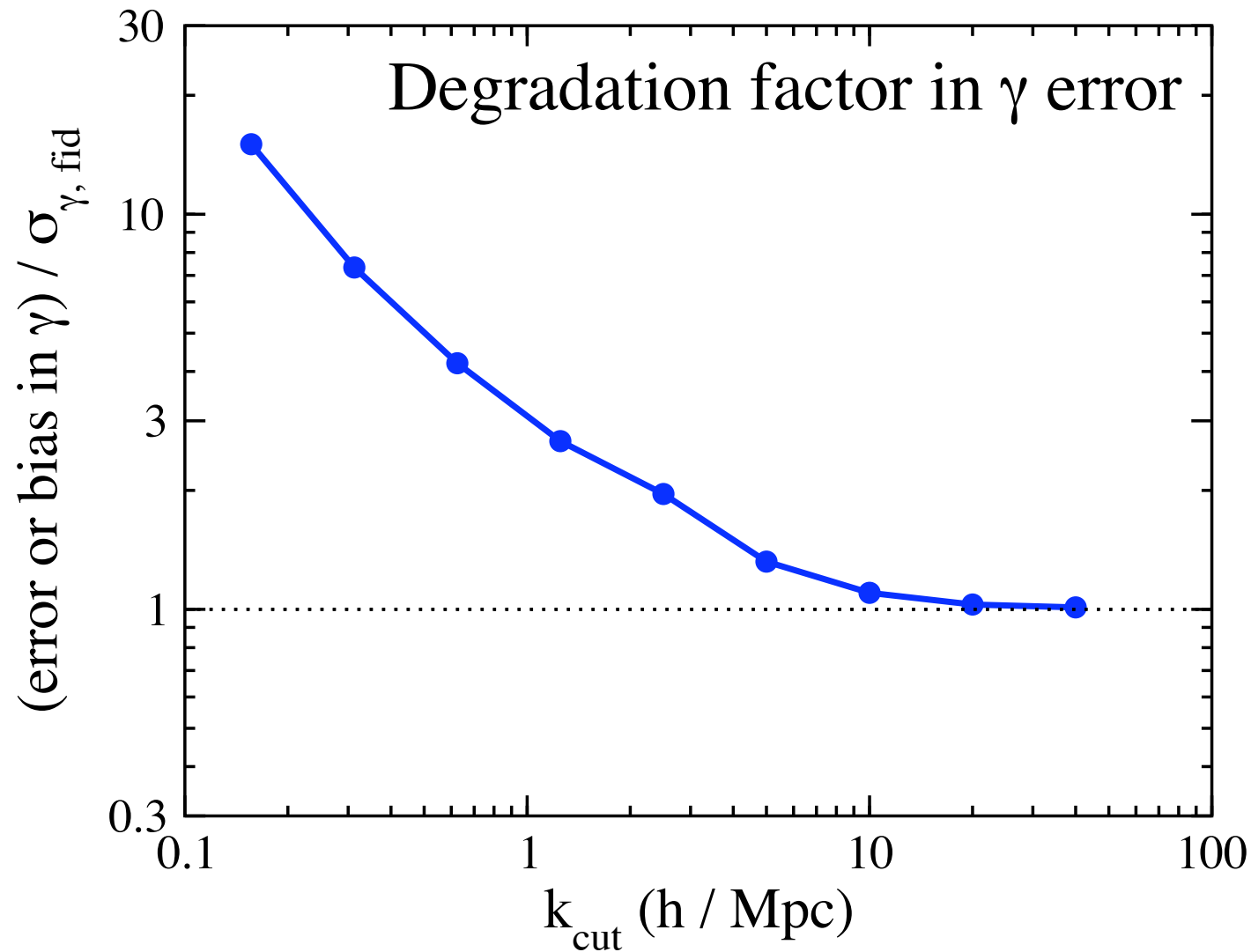


# Constraints on the growth index

	sig( $w_0$ )	sig( $w_a$ )	sig( $\gamma$ )
WL	0.33	1.16	0.23
+SNE	0.06	0.28	0.10
+Planck	0.06	0.21	0.044
+Clusters	0.05	0.16	0.037

Recall, for DGP  $\Delta\gamma = 0.13$

# Discarding the small-scale info in weak lensing

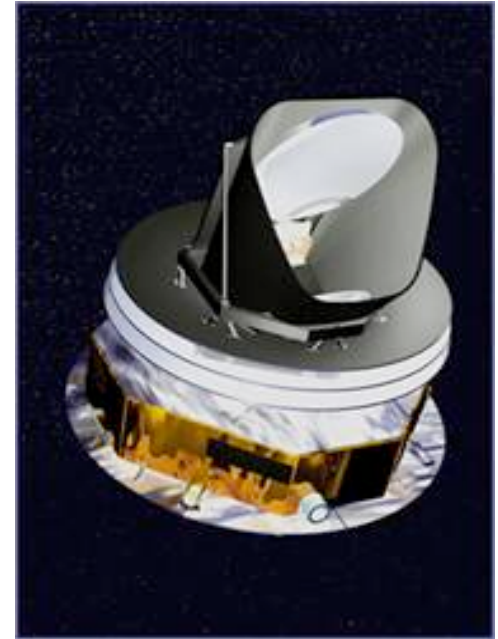


Using the Nulling Tomography of weak lensing (Huterer & White 2005)

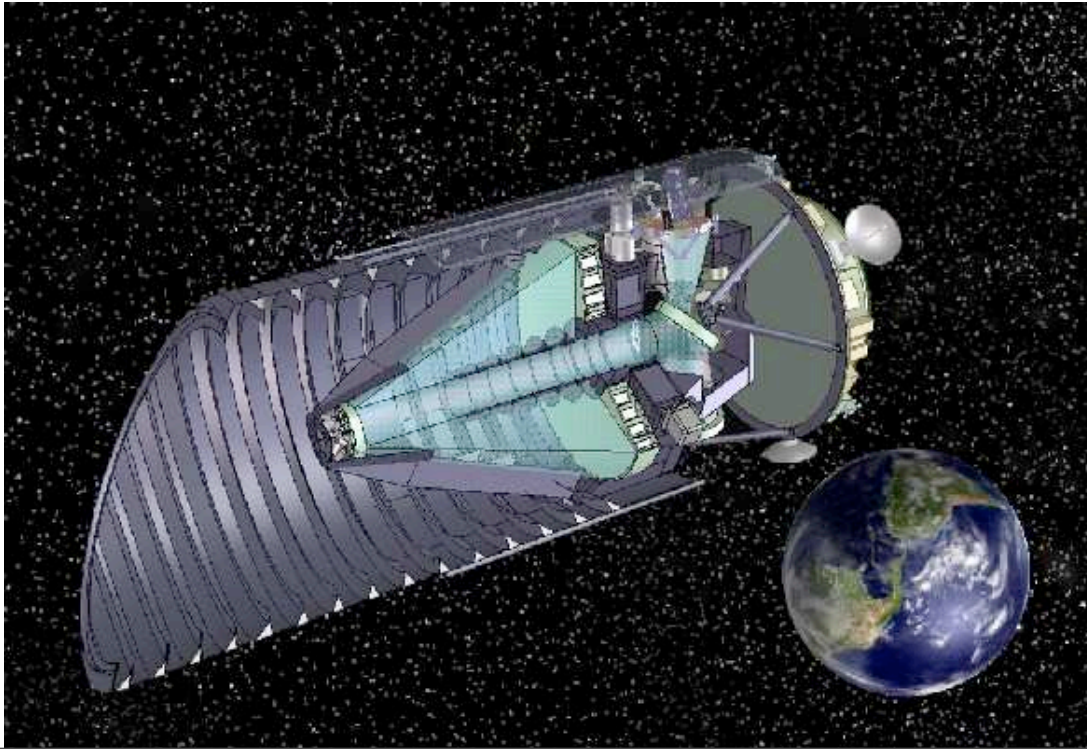
# South Pole Telescope



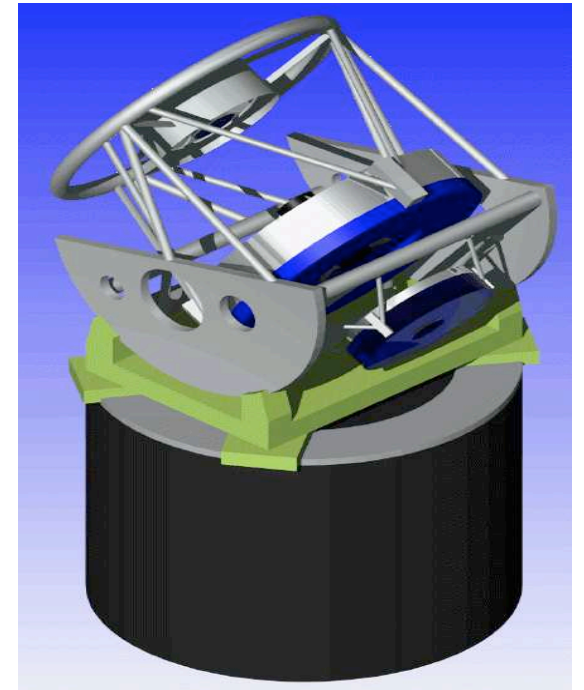
# Planck



# Supernova/Acceleration Probe



# LSST



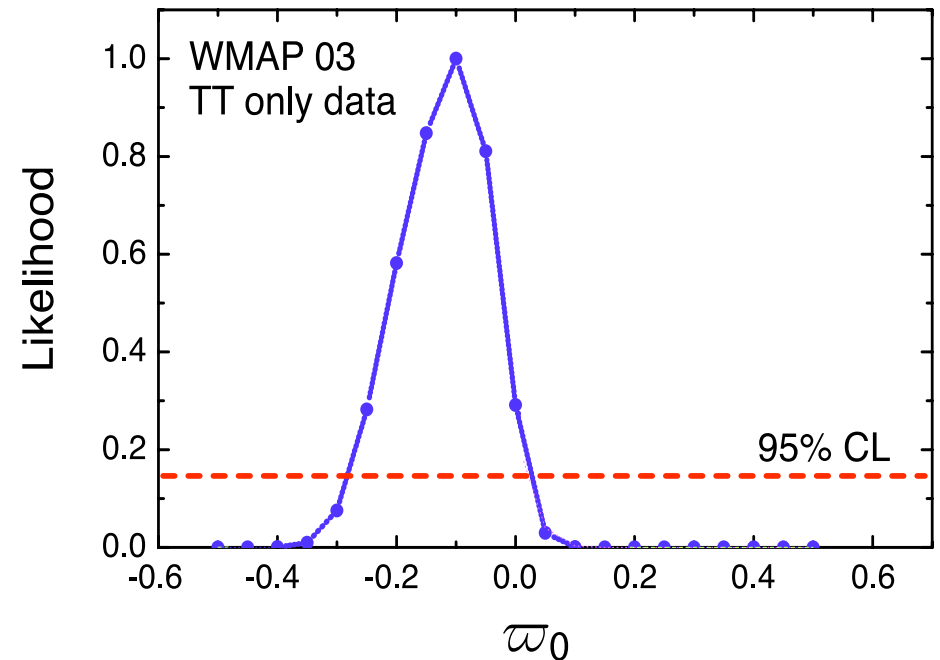
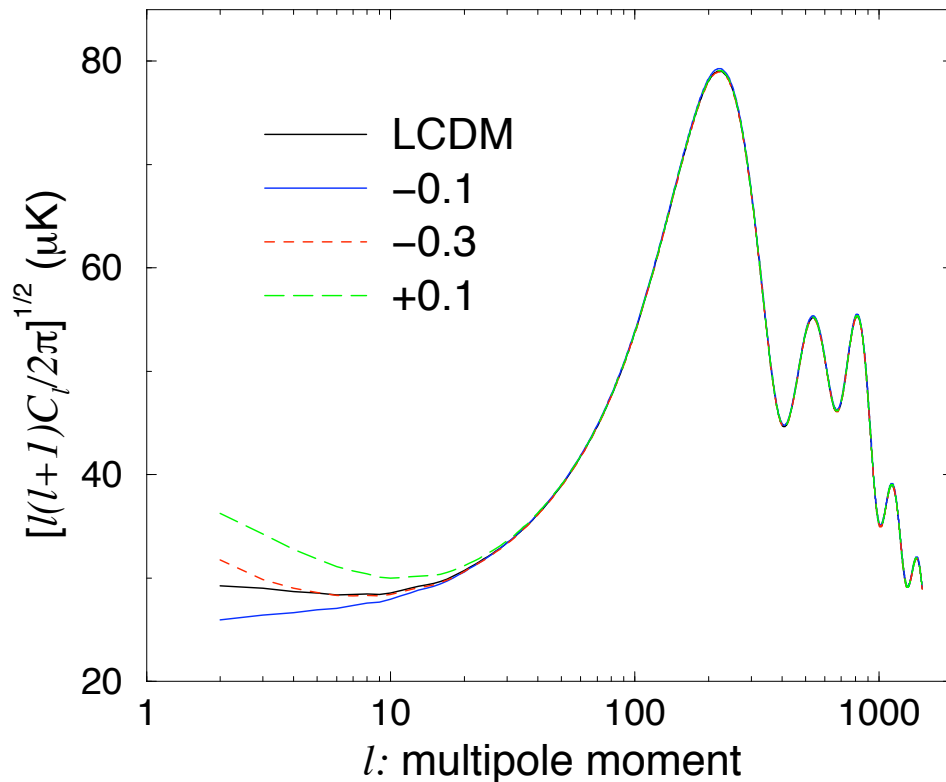
# Conclusions

- **distinguishing dark energy from modified gravity** is becoming one of the key goals of cosmology in years to come
- **assuming nonlinear clustering** that follows the usual prescription even with MG, we find that future probes can achieve very **interesting constraints** on this parameter
- **restriction to linear scales** severely degrades the errors, but well worth pursuing
- ambitious, general approach: measure functions  $r(z)$  and  $g(z)$ , check if they are consistent
- minimalistic approach: measure **a single parameter** that describes departures between DE and MG
- bright future with upcoming **powerful surveys**

# Physically motivated MG parametrization

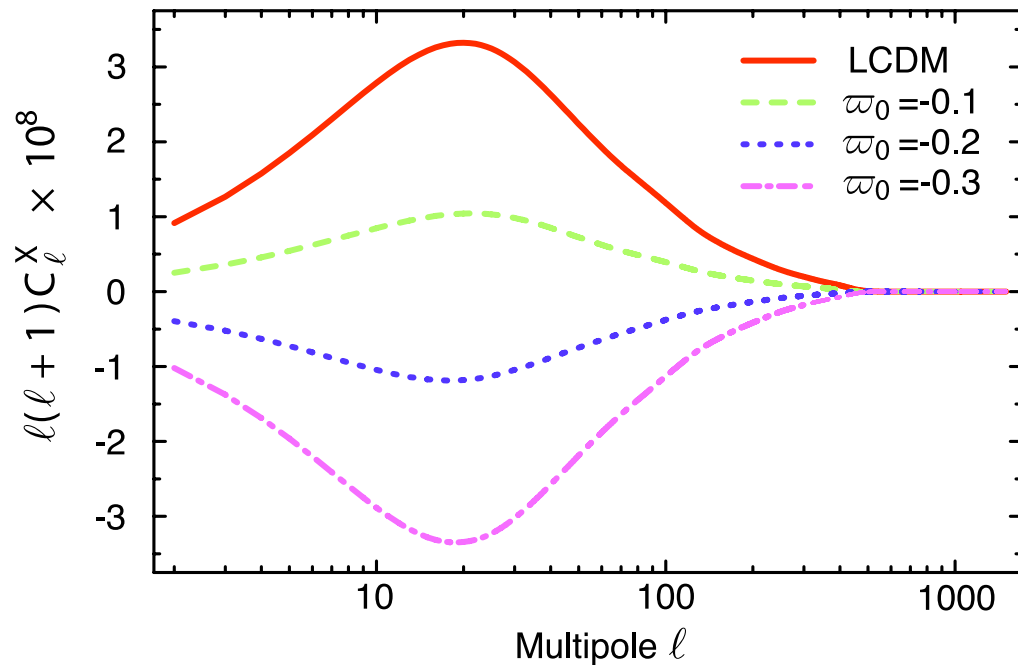
$$ds^2 = a^2(\tau) [-(1 + 2\psi)d\tau^2 + (1 - 2\phi)d\vec{x}^2]$$

$$\psi = (1 + \varpi)\phi \quad \text{and assume} \quad \varpi = \varpi_0 \frac{\rho_{DE}}{\rho_M}$$



# Physically motivated MG parametrization

## CMB-galaxy cross-correlation



## Weak lensing power spectrum

