



# Charm Decays

Karl M. Ecklund

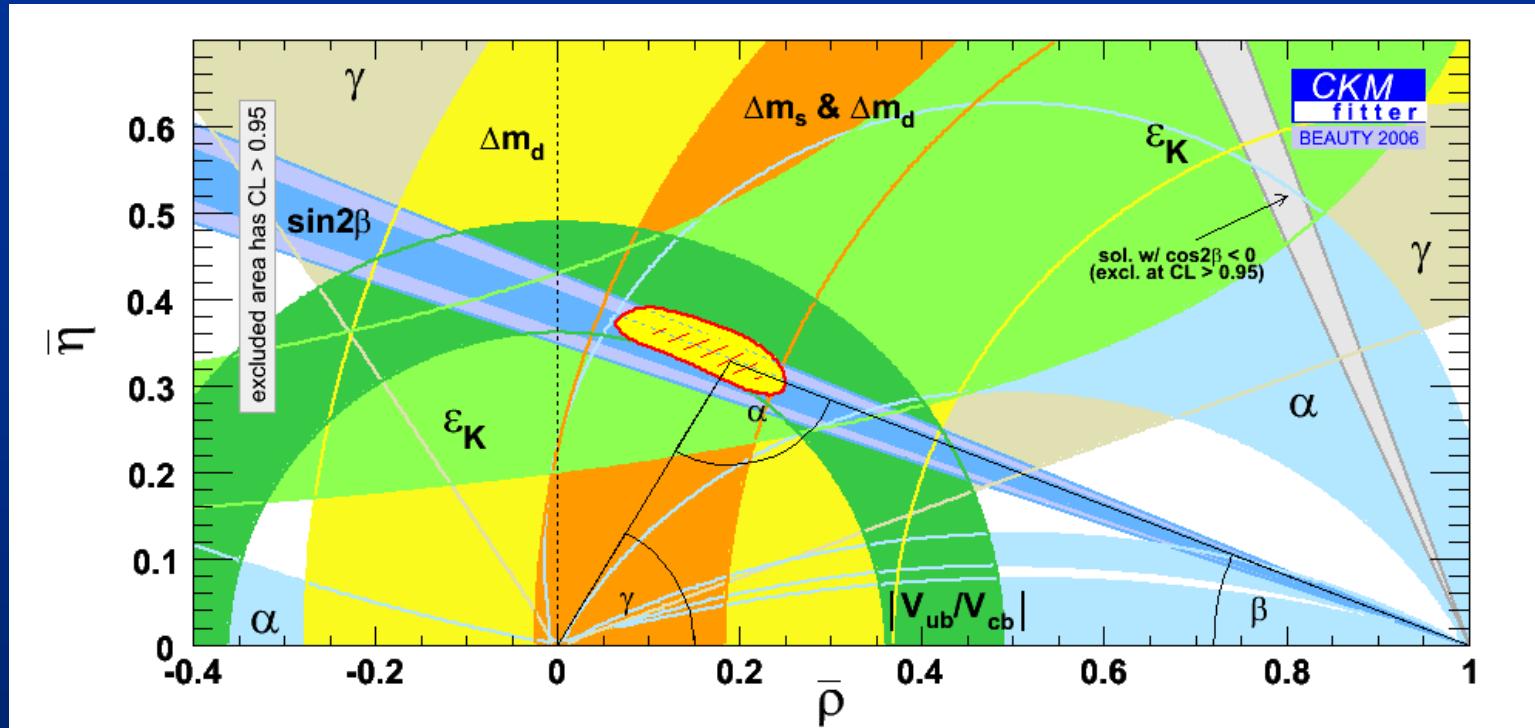


**University at Buffalo**  
*The State University of New York*

# Outline

- Results from active experiments
  - BaBar, Belle, CLEO-c, (CDF, DØ), FOCUS
- Guiding principle: Charm's role in flavor physics
- Hadronic Charm Decays
  - $D$  and  $D_s$  branching fractions
- Leptonic Charm Decays
  - decay constants from  $D_{(s)} \rightarrow \mu\nu$  and  $D_s \rightarrow \tau\nu$
- Semileptonic Charm Decays
  - branching fractions
  - hadronic form factors and CKM  $V_{cs}$  and  $V_{cd}$
- Many interesting results not shown for lack of time
  - hadronic structure in multibody decays
  - rare  $D$  decays: CDF  $D^0 \rightarrow \mu\mu$  search presented in session B14

# Charm's role in flavor physics



Flavor physics:

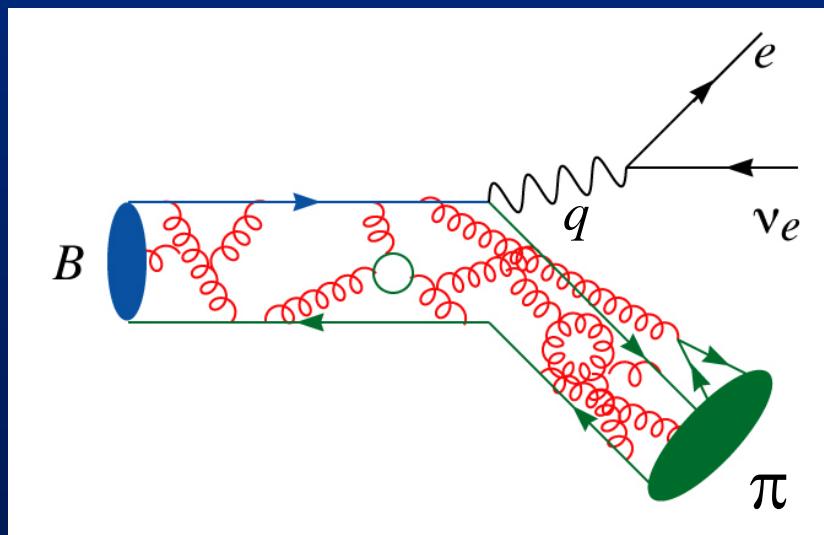
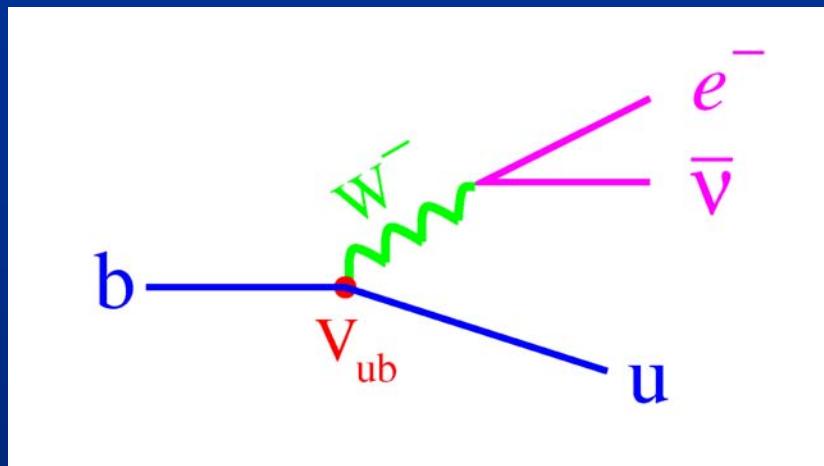
- Overconstrain  $V_{CKM}$
- Inconsistency  $\rightarrow$  new physics

Unitarity Triangle Constraints

- $\sin 2\beta$  is theoretically clean
  - $|V_{ub}|$  is not
  - $B$  mixing is not
- Hadronic uncertainties confound extraction of weak physics

Charm decay measurements can validate QCD corrections needed to extract weak physics parameters from experimental observables

# $|V_{ub}|$ from semileptonic B decay



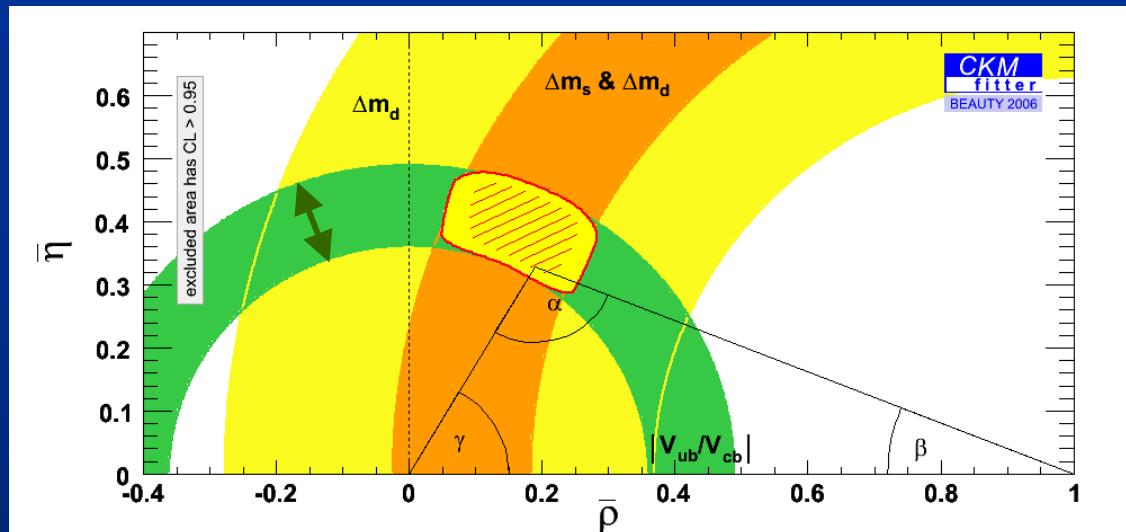
If quarks were like muons:

$$\Gamma(b \rightarrow ue\nu) = \frac{G_F^2 m_b^5}{192\pi^3} |V_{ub}|^2$$

- Rate goes like  $|V_{ub}|^2$
- But quarks always in hadrons
- QCD form factor  $f_+(q^2)$  needed to extract weak interaction physics

$$\frac{d\Gamma}{dq^2} = \frac{G_F^2}{24\pi^3} |V_{ub}|^2 p_\pi^3 |f_+(q^2)|^2$$

# UT Constraint from $|V_{ub}|$



$|V_{ub}|$  from  $B \rightarrow \pi \ell \nu$ :

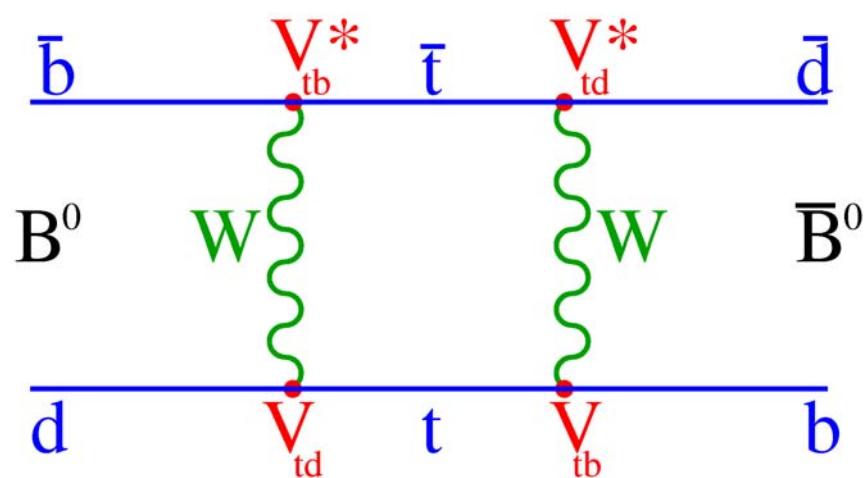
$$\frac{d\Gamma}{dq^2} = \frac{G_F^2}{24\pi^3} |V_{ub}|^2 p_\pi^3 |f_+(q^2)|^2$$

Form factor  $f(q^2)$ :

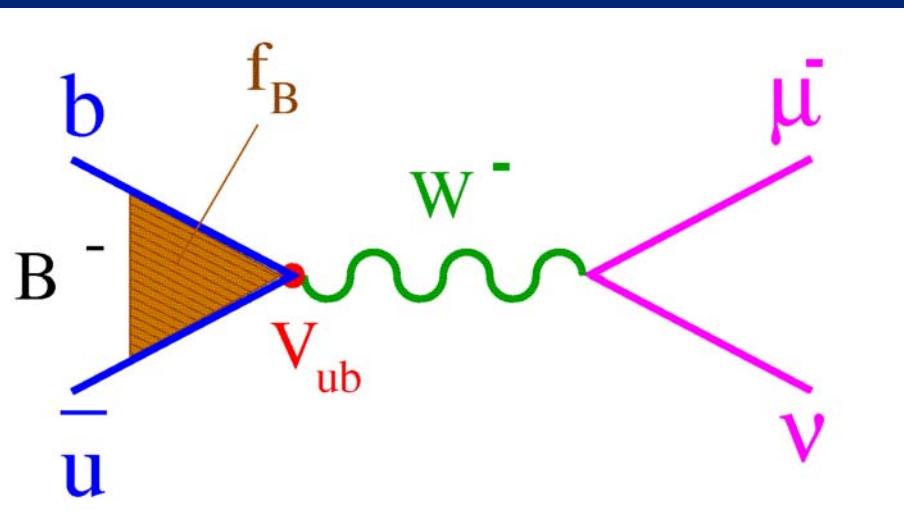
- Hard to calculate
- Limits  $|V_{ub}|$  precision
- Lattice QCD can do from first principles

- $D \rightarrow \pi \ell \nu$  to  $B \rightarrow \pi \ell \nu$  are both "heavy to light" decays
- Precise measurement of  $D \rightarrow \pi \ell \nu$  can calibrate LQCD and allow a precise extraction of  $|V_{ub}|$  from  $B \rightarrow \pi \ell \nu$
- Absolute rate and shape is a stringent test of theory

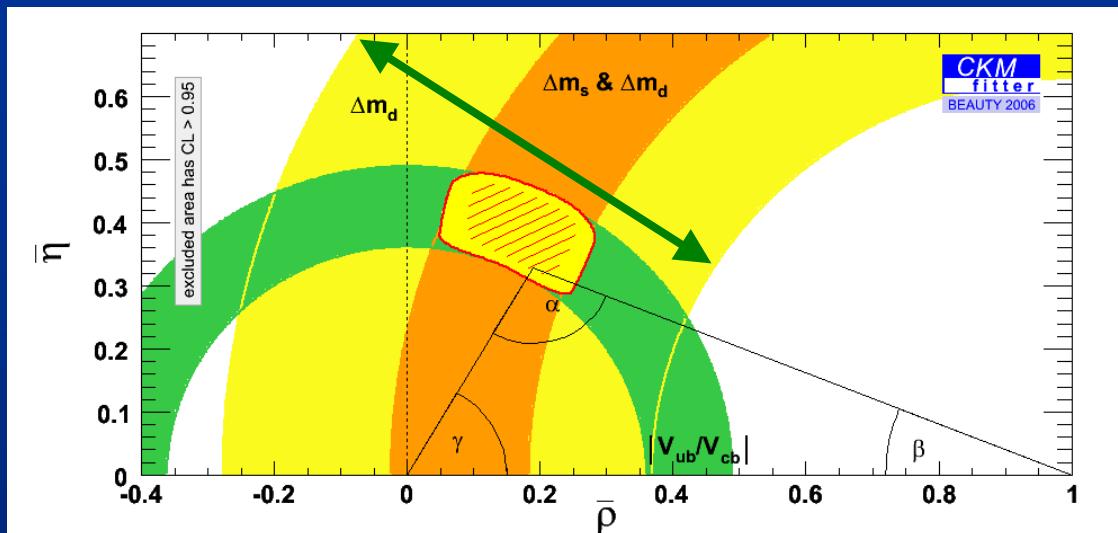
# $|V_{td}|$ from $B^0-\overline{B}{}^0$ mixing



- Mixing rate depends on  $|V_{td}|^2$
- QCD correction here is partly decay constant  $f_B$ 
  - probability of wave function overlap  $\psi(r=0)$
- Hard to calculate @ small  $q^2$  low energy QCD
  - Lattice QCD to  $\sim 15\%$
- Same for meson decay
- Can measure annihilation decay
  - Belle: PRL 97, 251802 (2006)  
Evidence for  $B^- \rightarrow \tau^- \nu$  ( $3.5 \sigma$ )  
 $f_B = 229 \pm 36 \pm 37$  MeV (20%)
- But would like a *precise* measurement



# UT Constraint from B mixing



$$\Delta M_d = 0.50 \text{ ps}^{-1} \left[ \frac{\sqrt{B_{B_d}} f_{B_d}}{200 \text{ MeV}} \right]^2 \left[ \frac{|V_{td}|}{8.8 \times 10^{-3}} \right]^2$$

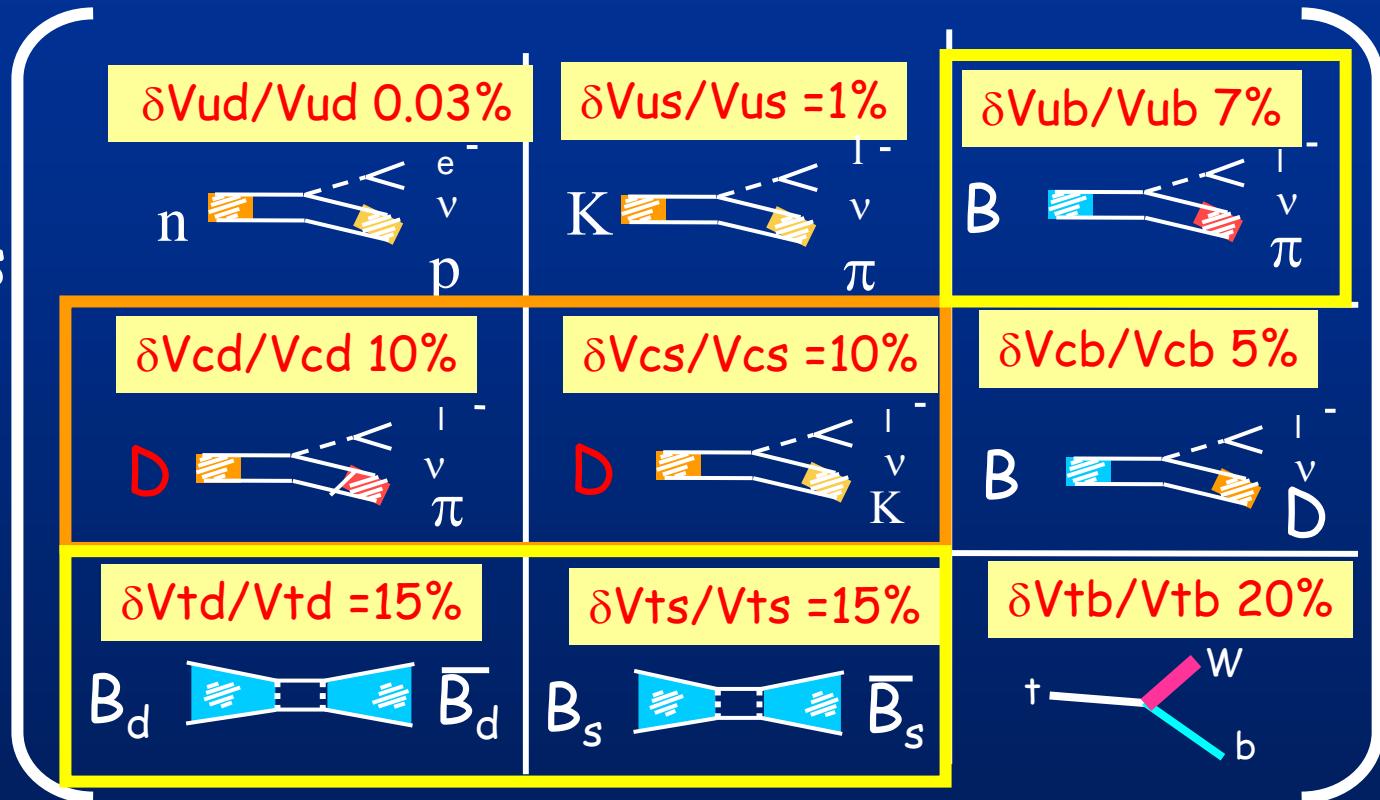
$$\frac{\sigma(|V_{td}|)}{|V_{td}|} = 0.5 \frac{\sigma(\Delta M_d)}{\Delta M_d} \oplus \frac{\sigma(f_B \sqrt{B_{B_d}})}{f_B \sqrt{B_{B_d}}}$$

0.8% ~15% (LQCD)

- Lattice QCD predicts decay constants  $f_D$  &  $f_B$
- Charm sector measurements of  $f_{D(s)}$  from  $D_{(s)} \rightarrow \mu\nu$  can increase our confidence in the non-perturbative QCD calculations of  $f_B$  needed to interpret  $\Delta m$  and  $\Delta m_s$ 
  - direct measurement of  $B \rightarrow \ell\nu$  is much harder!
- Better constraint on  $|V_{ts}/V_{td}|$  from  $\Delta m_s/\Delta m_d$ 
  - still want to check  $f_{Ds}/f_D$

# CKM Matrix

Current  $V_{CKM}$   
From direct  
Measurements  
-no unitarity  
imposed



charm decay measurements:

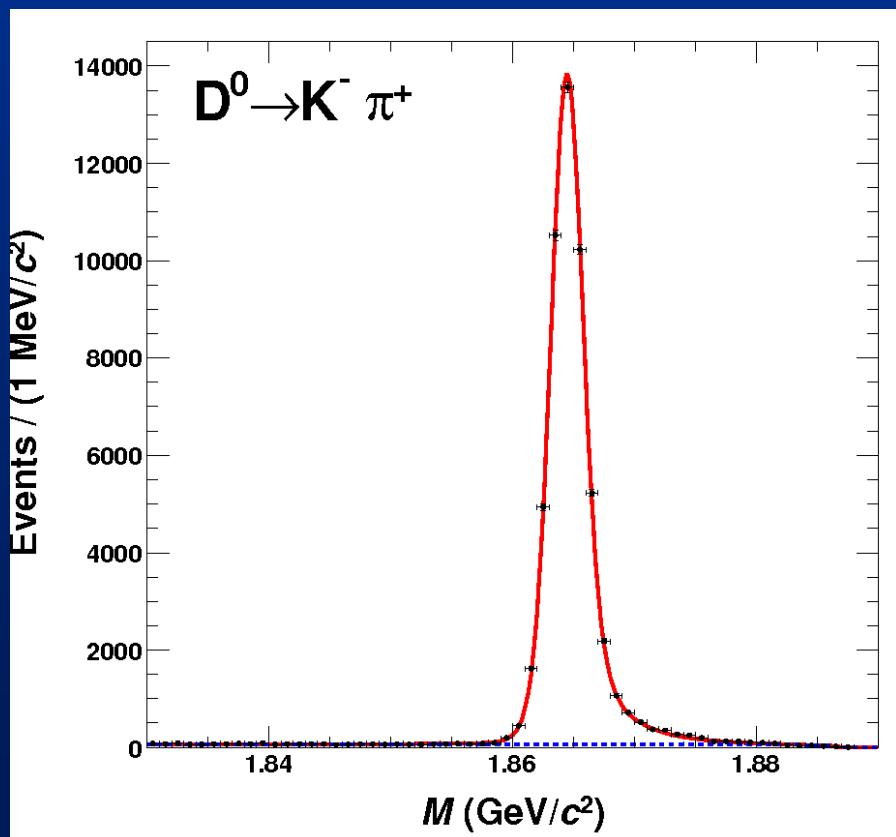
- direct access to 2<sup>nd</sup> generation elements
- enable improvements in 3<sup>rd</sup> generation elements

# CLEO-c Hadronic D Decays

Presented in session B14 X.Shi

$$e^+e^- \rightarrow \psi(3770) \rightarrow D \bar{D} \quad (D^0\bar{D}^0 \text{ or } D^+\bar{D}^-)$$

- Just above threshold: no additional particles are produced
- Fully reconstruct one D in the event, e.g.  $D^0 \rightarrow K^- \pi^+$



Energy and Momentum  
Conservation:

$$E_D = E_K + E_\pi$$

$$\vec{p}_D = \vec{p}_K + \vec{p}_\pi$$

$$\Delta E = E_{\text{beam}} - E_D$$

$$M(D) = \sqrt{E_{\text{beam}}^2 - |\vec{p}_D|^2}$$

resolution:  
7-10 MeV

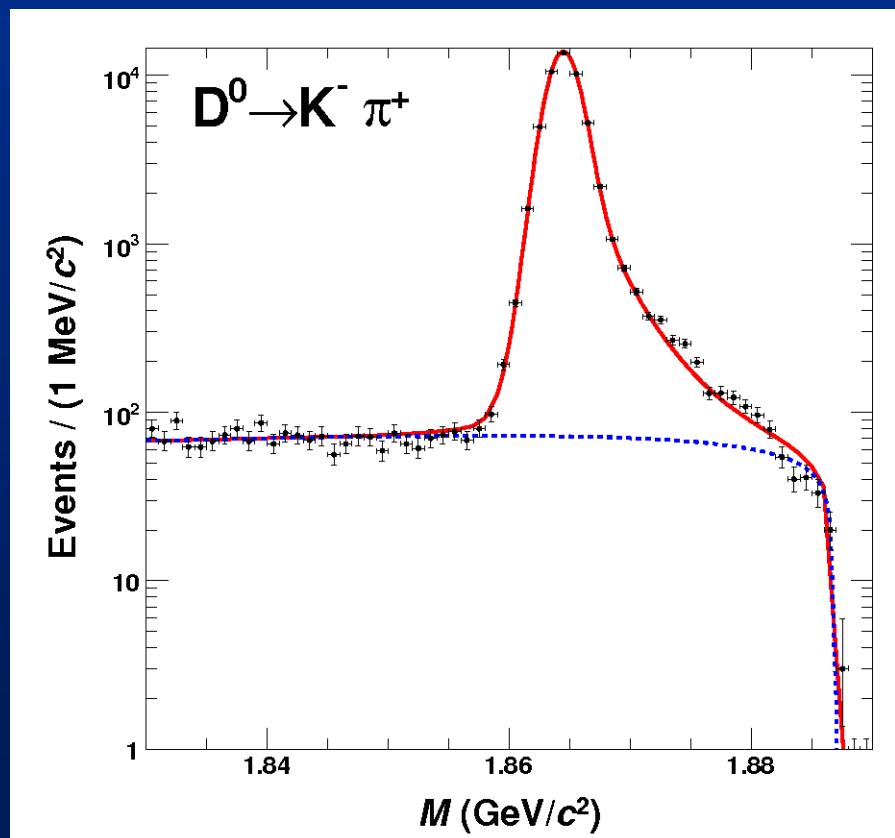
1.3 MeV

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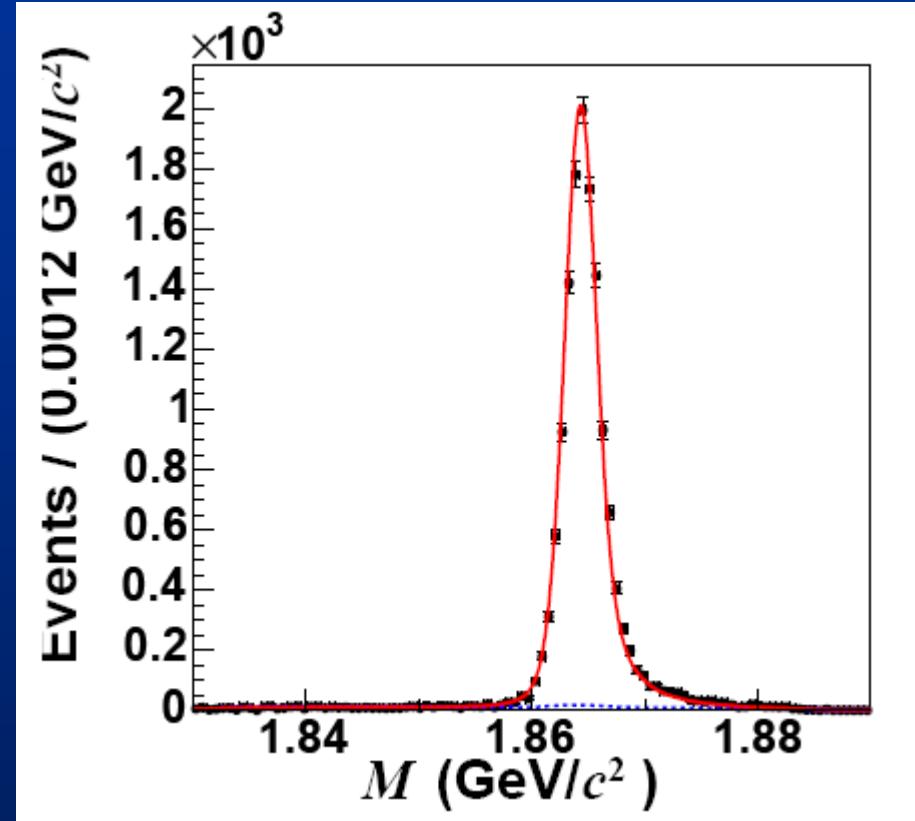
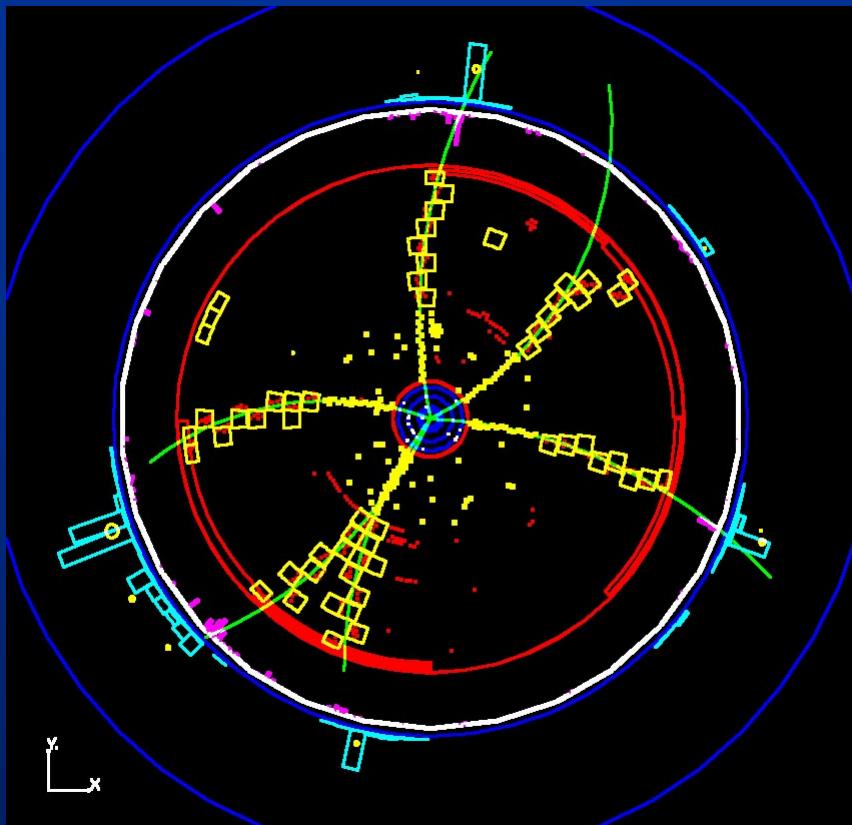
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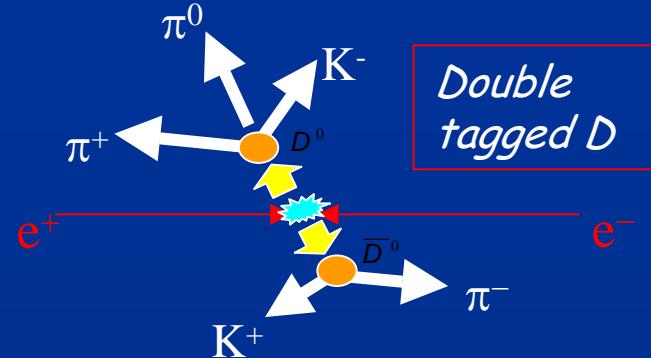
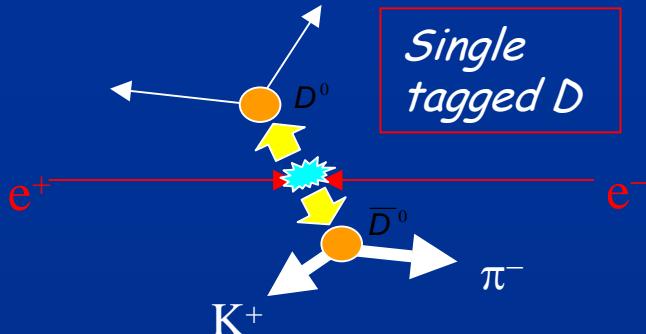
# Double Tag Events



$$D^+ \rightarrow K^-\pi^+\pi^+ \text{ & } D^- \rightarrow K^+\pi^-\pi^-$$

- Tagging effectively makes a single D beam
- Can tag  $\approx 22\%$  of D's produced!

$$\mathcal{B}(D \rightarrow X_i) = \frac{N(D \rightarrow X_i)}{\text{Efficiency} \times N_{\text{tags}}}$$



$$N_i = N_{D\bar{D}} B_i \varepsilon_i$$

$$N_{ij} = N_{D\bar{D}} B_i B_j \varepsilon_{ij}$$

$$B_i = \frac{N_{ij}}{N_j} \frac{\varepsilon_j}{\varepsilon_{ij}}$$

$$N_{D\bar{D}} = \frac{N_i N_j}{N_{ij}} \frac{\varepsilon_{ij}}{\varepsilon_i \varepsilon_j}$$

$$\varepsilon_{ij} \approx \varepsilon_i \varepsilon_j$$

$$\varepsilon_i = 16 - 65\%$$

9 modes, simultaneous  $\chi^2$  fit  
including correlations on  $N$ ,  $\varepsilon$   
to extract 9  $B_i$  &  $N(D\bar{D})$

D Decay Mode
$K^- \pi^+$
$K^- \pi^+ \pi^0$
$K^- \pi^+ \pi^+ \pi^-$
$K^- \pi^+ \pi^+$
$K^- \pi^+ \pi^+ \pi^0$
$K_S^0 \pi^+$
$K_S^0 \pi^+ \pi^0$
$K_S^0 \pi^+ \pi^+ \pi^-$
$K^+ K^- \pi^+$

56 pb<sup>-1</sup>: PRL 95 121801 (2005)

281 pb<sup>-1</sup>: Preliminary results

reported at this meeting (X. Shi)

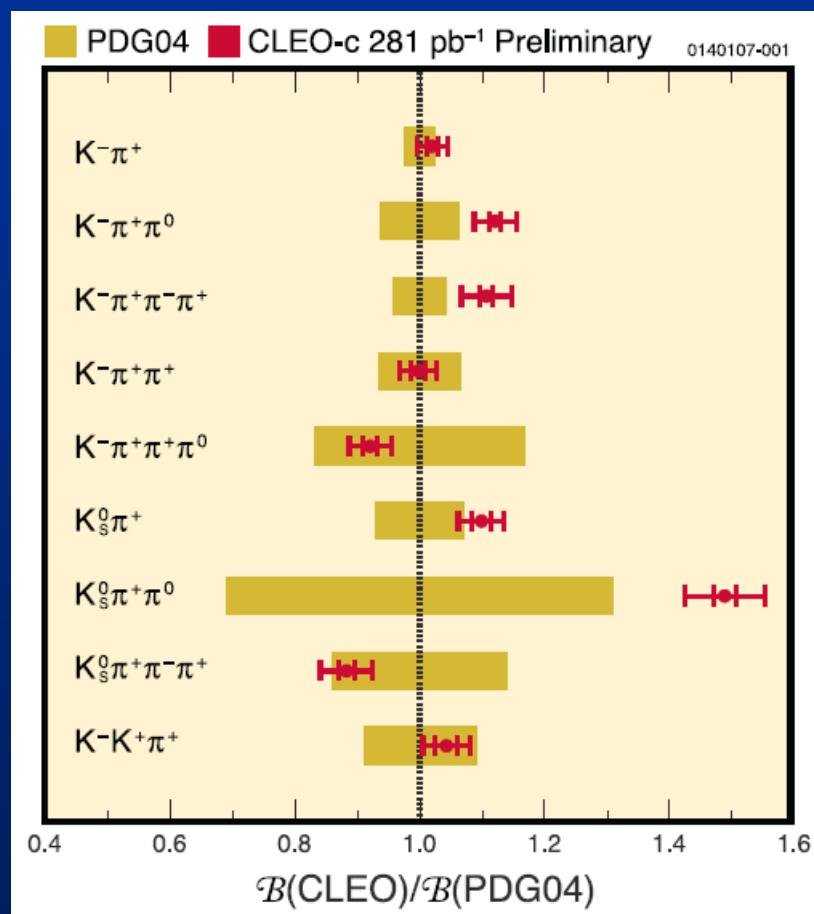
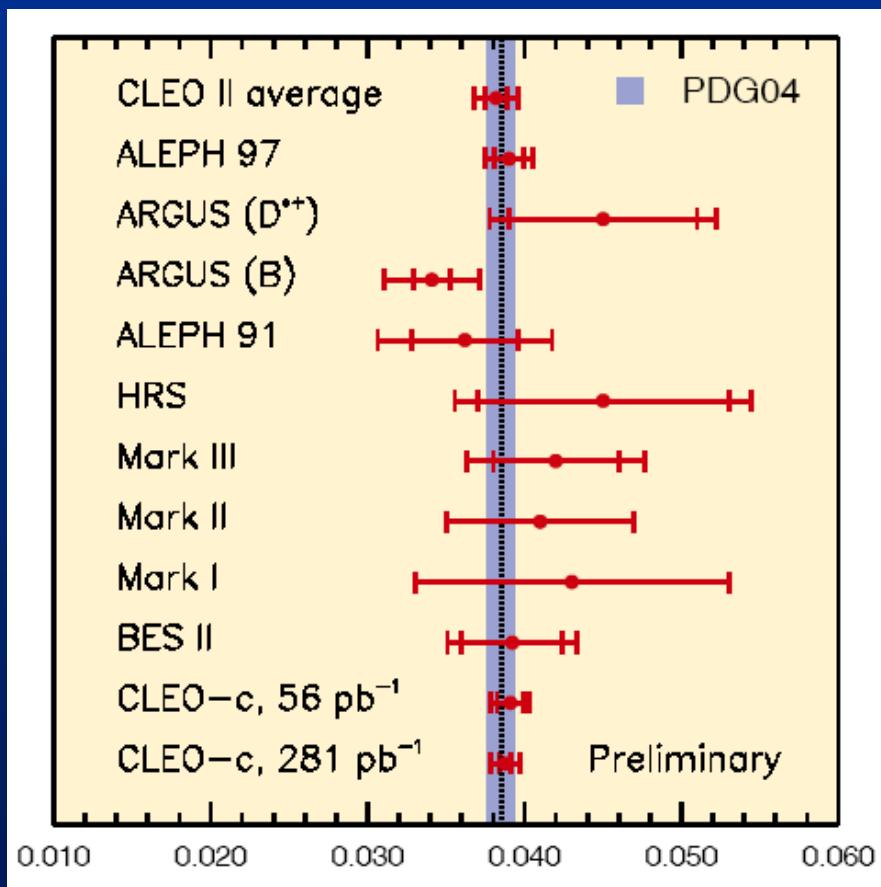
Additional data in hand now ( $\sim 280$  pb<sup>-1</sup>)

And from run through Mar'08 ( $\sim 300$  pb<sup>-1</sup>)

# CLEO-c hadronic decay results

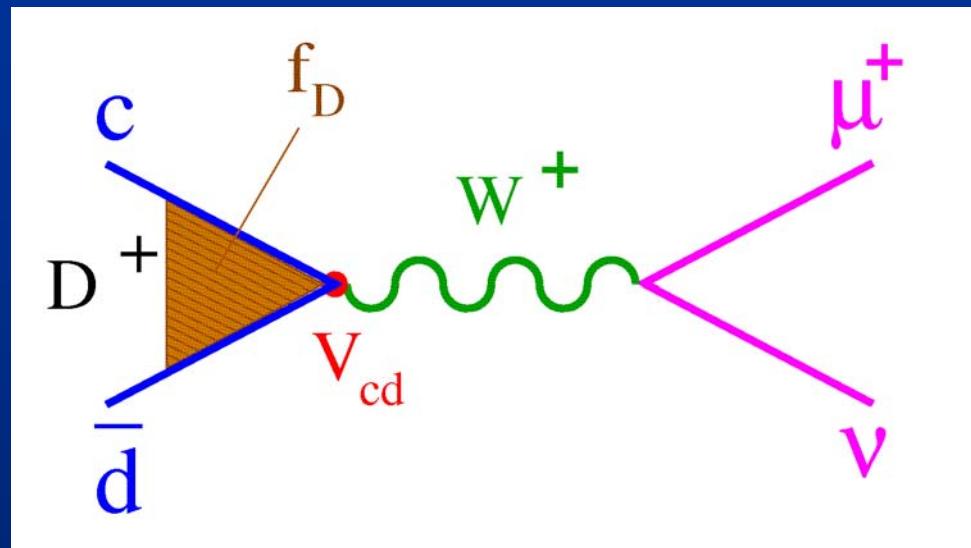
Comparison to other measurements

$$\text{BF}(D^0 \rightarrow K^-\pi^+)$$



Precision measurements of many  
 $D^0, D^+$  decay modes

# Leptonic $D_{(s)}$ Decay



- Measure rate to extract  $f_D$  and  $f_{D_s}$
- Useful to calibrate  $V_{td}/V_{ts}$  from  $B_{(s)}^0$  mixing

$$\mathcal{B}(D \rightarrow \mu\nu) = \Gamma \tau_D \approx 4 \times 10^{-4}$$

$$\mathcal{B}(D \rightarrow \tau\nu) \approx 4 \times 10^{-3}$$

$$\mathcal{B}(D_s \rightarrow \mu\nu) \approx 6 \times 10^{-3}$$

$$\mathcal{B}(D_s \rightarrow \tau\nu) \approx 6 \times 10^{-2}$$

$$\Gamma(D \rightarrow \mu\nu) = \frac{G_F^2}{8\pi} |V_{cd}|^2 f_D^2 m_\mu^2 M_D^2 \left(1 - \frac{m_\mu^2}{M_D^2}\right)^2$$

↑

decay constant

measures overlap of quark wave functions

CLEO-c  $D^+ \rightarrow \mu\nu$ 281 pb<sup>-1</sup> PRL 95, 251801 (2005)Use 158k tagged D<sup>-</sup> decays

Require

- one  $\mu$  candidate with MIP-like shower
- no extra tracks
- no unmatched showers with  $E_{CC} > 250$  MeV

$$\mathcal{B} = (4.40 \pm 0.66^{+0.09}_{-0.12}) \times 10^{-4}$$

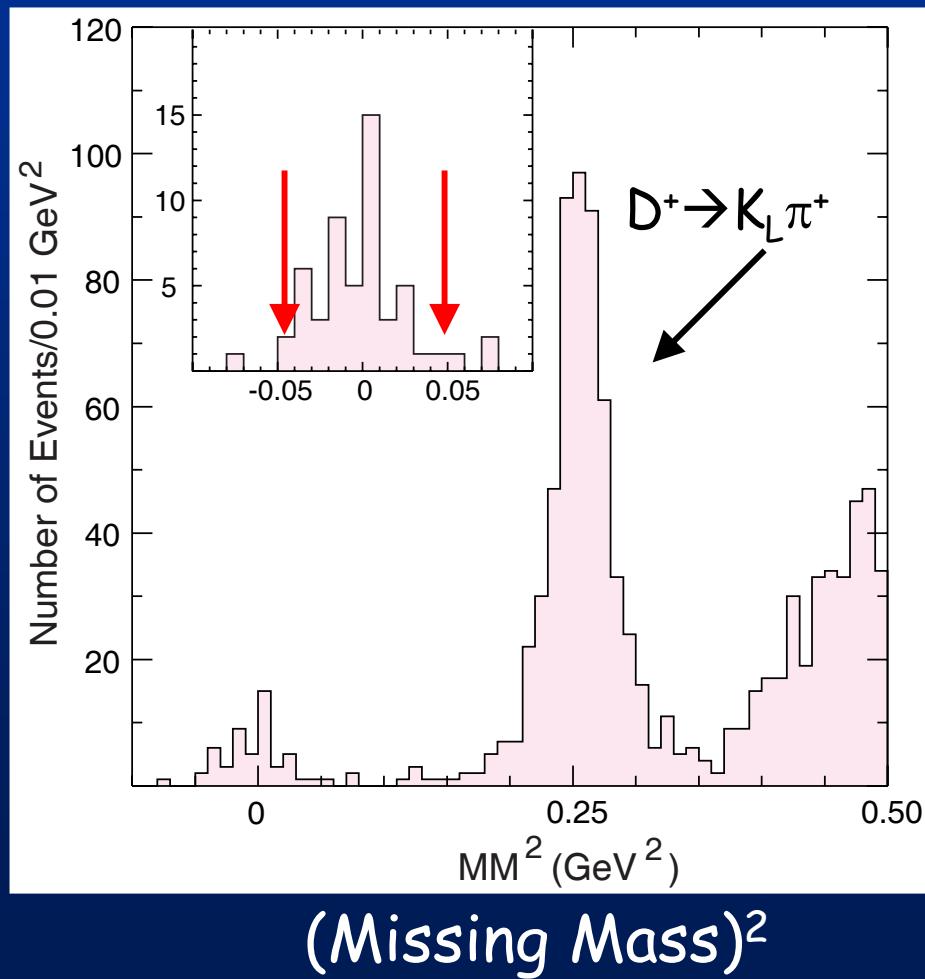
$$f_D = (222.6 \pm 16.7^{+2.8}_{-3.4}) \text{ MeV}$$

Unquenched Lattice QCD

 $201 \pm 3 \pm 17$  MeV

PRL 95, 122002 (2005)

signal region: 50 events  
 2.8 estimated background



$e^+e^- \rightarrow D_s^* D_{\text{tag}} X$ ;  $D_{\text{tag}}$  is fully reconstructed  $D_{(s)}^{(*)}$   
 Then look for  $D_s^* \rightarrow D_s \gamma$ ;  $D_s \rightarrow \mu\nu$ :

$\Delta M = M(\mu\nu\gamma) - M(\mu\nu)$  signal peak at 143 GeV

- Measure also  $D_s \rightarrow \phi\pi$  to normalize
- Detailed systematic understanding

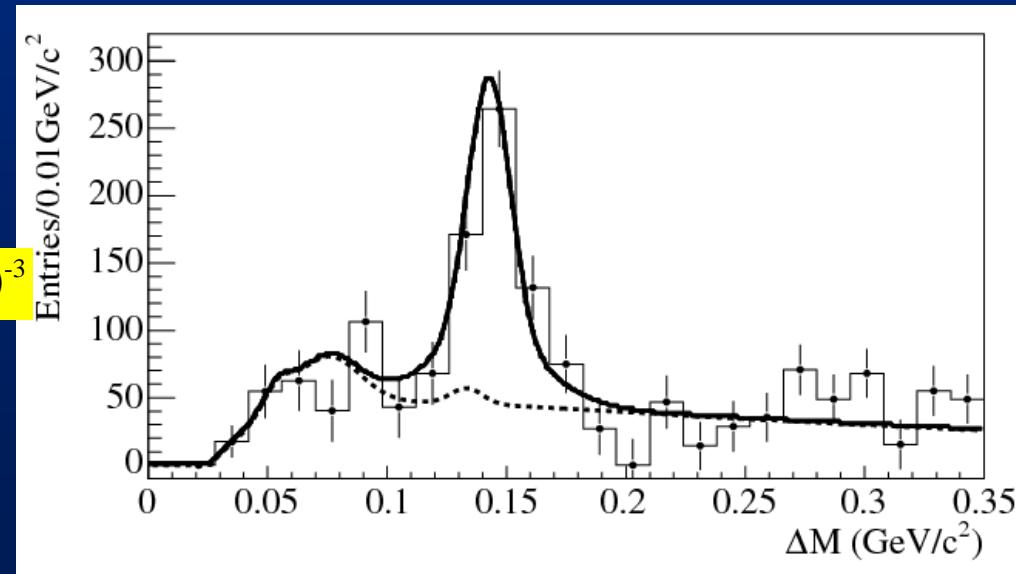
$$\frac{\Gamma(D_s^+ \rightarrow \mu^+\nu)}{\Gamma(D_s^+ \rightarrow \phi\pi^+)}$$

$$= 0.143 \pm 0.018 \pm 0.006$$

$$BF(D_s \rightarrow \mu\nu) = (6.74 \pm 0.83 \pm 0.26 \pm 0.66) \times 10^{-3}$$

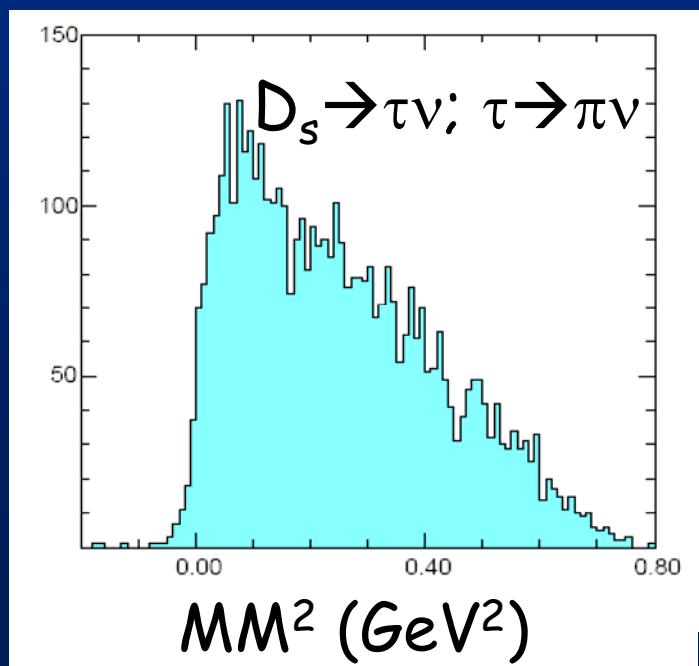
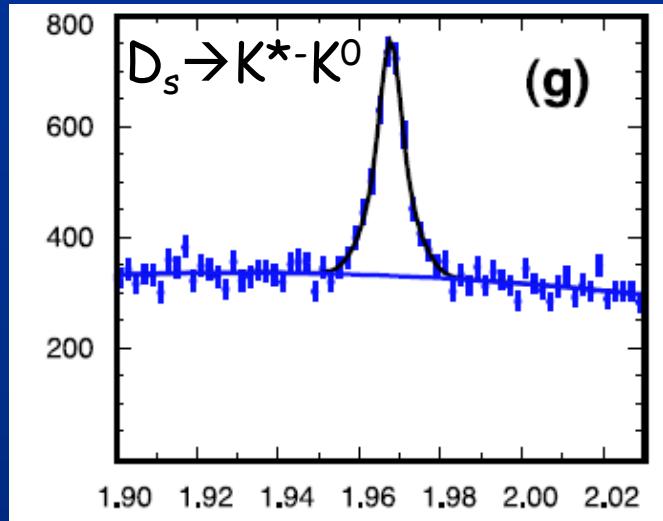
$$f_{D_s} = (283 \pm 17 \pm 7 \pm 14) \text{ MeV}$$

Unquenched Lattice QCD  
 $249 \pm 3 \pm 16$  MeV  
 PRL 95, 122002 (2005)



# CLEO-c $D_s \rightarrow \mu\nu$ & $D_s \rightarrow \tau\nu$ ; $\tau \rightarrow \pi\nu$

- $e^+e^- \rightarrow D_s D_s^*$  @  $\sqrt{s}=4170$  MeV  
314 pb<sup>-1</sup>
- Fully Reconstruct
  - 19k  $D_s$  tags (8 modes)
  - Recoil Mass peaks at  $D_s^*$ 
    - count tags by fit
- Add a single track
  - $\mu$ : MIP-like in Calorimeter
  - $\pi$ : sometimes  $E_{CC} > 200$  MeV
  - $MM^2$  peaks at 0 for  $\mu\nu$
  - and near 0 for  $\tau\nu$ ;  $\tau \rightarrow \pi\nu$
- Veto events with
  - extra tracks
  - extra neutral energy
- Kinematic Fit
  - improved resolution
  - resolve ambiguity:  $D_s^* \rightarrow D_s \gamma$   
on tag or signal side



CLEO-c  $f_{D_s}$  Results

Case	Region ( $\text{GeV}^2$ )	Signal	Background
i	$-0.05 < \text{MM}^2 < 0.05$	92	$3.5 \pm 1.4$
i	$0.05 < \text{MM}^2 < 0.20$	31	$2.5 \pm 1.1$
ii	$-0.05 < \text{MM}^2 < 0.20$	25	$3.0 \pm 1.3$
Sum	$-0.05 < \text{MM}^2 < 0.20$	148	$9.0 \pm 2.3$

arXiv:0704.0437 (to PRD)

arXiv:0704.0629 (to PRL)

$$\mathcal{B} = (0.638 \pm 0.059 \pm 0.033)\%$$

$$f_{D_s} = (274 \pm 13 \pm 7) \text{ MeV}$$

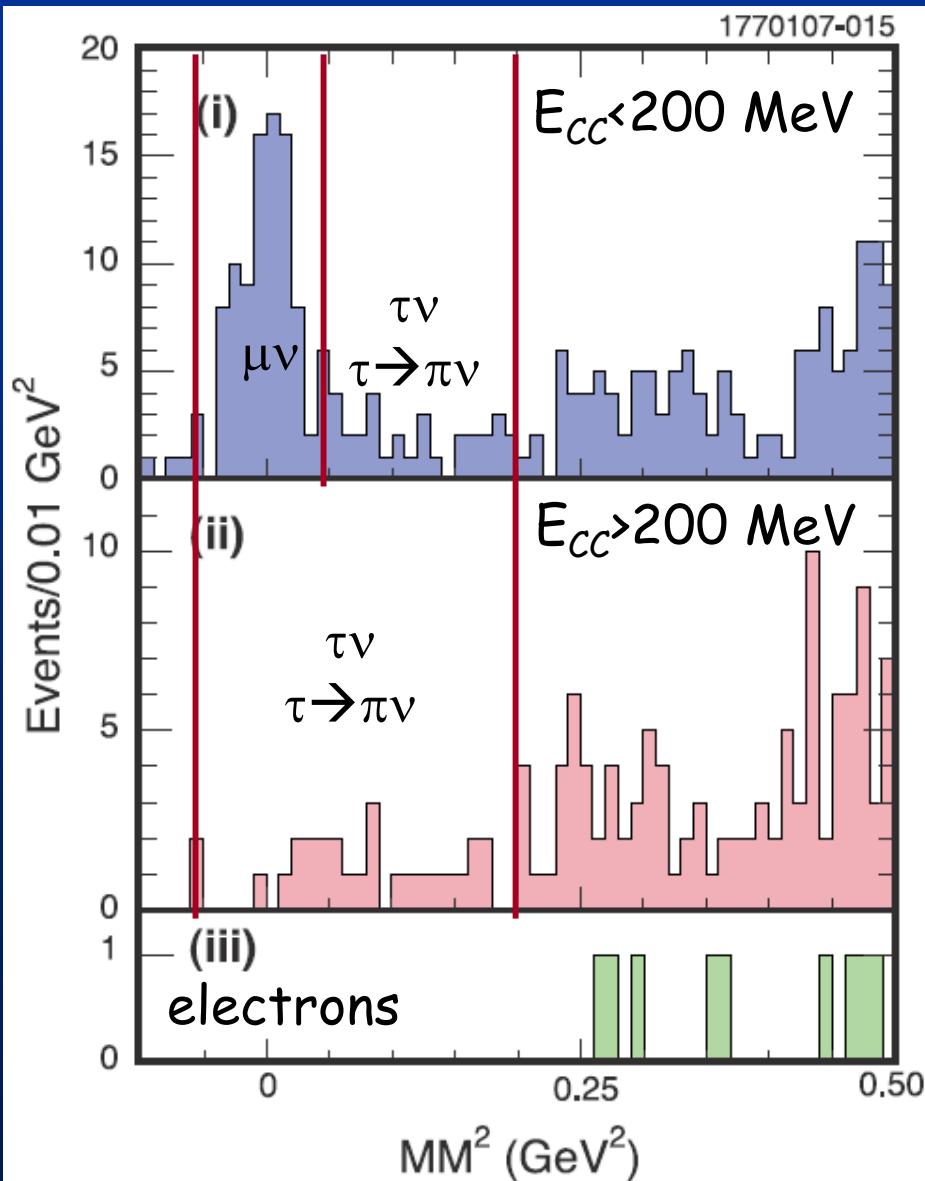
Unquenched Lattice QCD

 $249 \pm 3 \pm 16 \text{ MeV}$ 

PRL 95, 122002 (2005)

$$\frac{f_{D_s}}{f_D} = 1.23 \pm 0.11 \pm 0.04$$

ULQCD  
 $1.24 \pm 0.01 \pm 0.07$



# CLEO-c $D_s^+ \rightarrow \tau^+\nu; \tau^+ \rightarrow e^+\nu\nu$

## 2<sup>nd</sup> Complementary Analysis with $\tau^+ \rightarrow e^+\nu\nu$

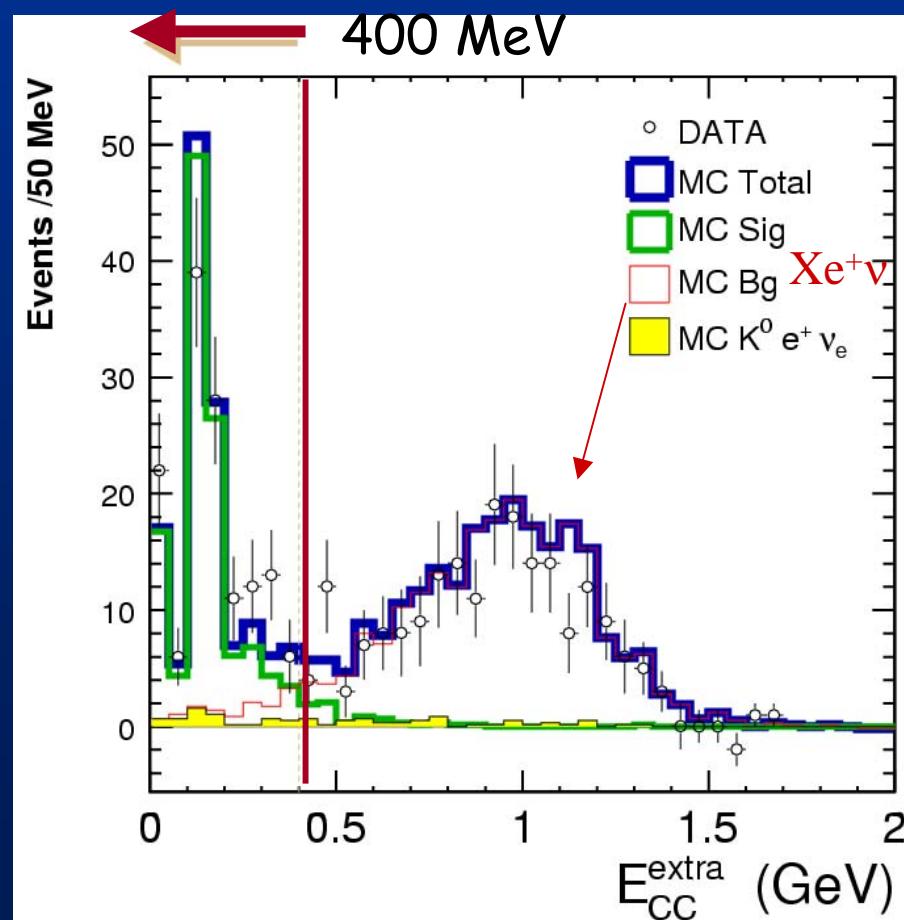
- Signal production of  $e^+$ :  $B(D_s^+ \rightarrow \tau^+\nu)B(\tau^+ \rightarrow e^+\nu\nu) \sim 1.3\%$
- Background:  $B(D_s^+ \rightarrow Xe^+\nu) \sim 8\%$

### Technique:

- Use  $D_s^-$  tags and  $e^+$
- Suppress background
  - no additional tracks and
  - $\sum E_{\text{cal}} < 400 \text{ MeV}$
- No need to find  $\gamma$  from  $D_s^*$
- $B(D_s^+ \rightarrow \tau^+\nu) = (6.29 \pm 0.78 \pm 0.52)\%$
- $f_{D_s} = 278 \pm 17 \pm 12 \text{ MeV}$

Preliminary @ ICHEP 06

195 pb<sup>-1</sup> near  $\sqrt{s} = 4170 \text{ MeV}$



# $f_{D(s)}$ : Comparison to Theory

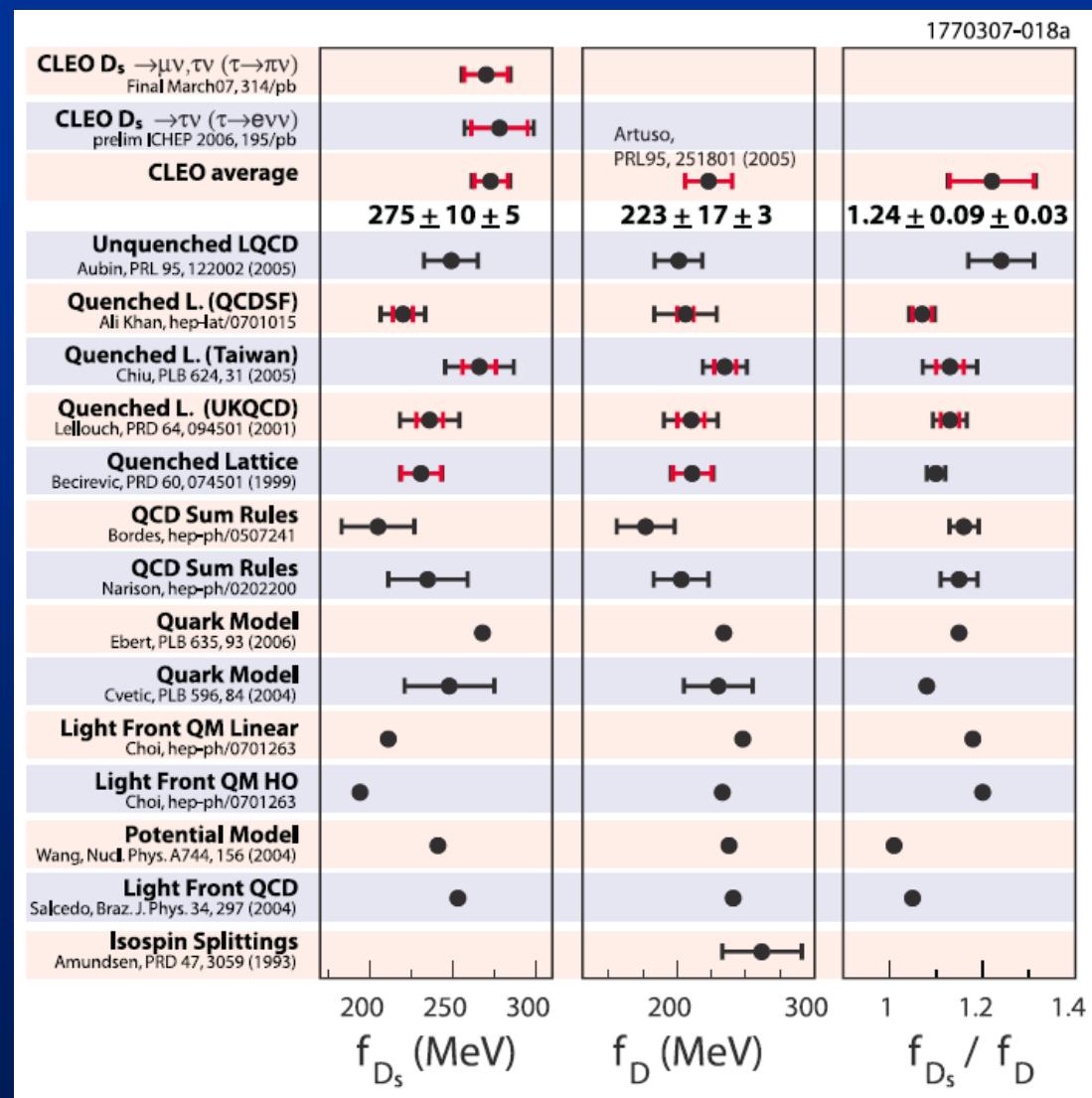
CLEO results

- Good agreement with unquenched LQCD

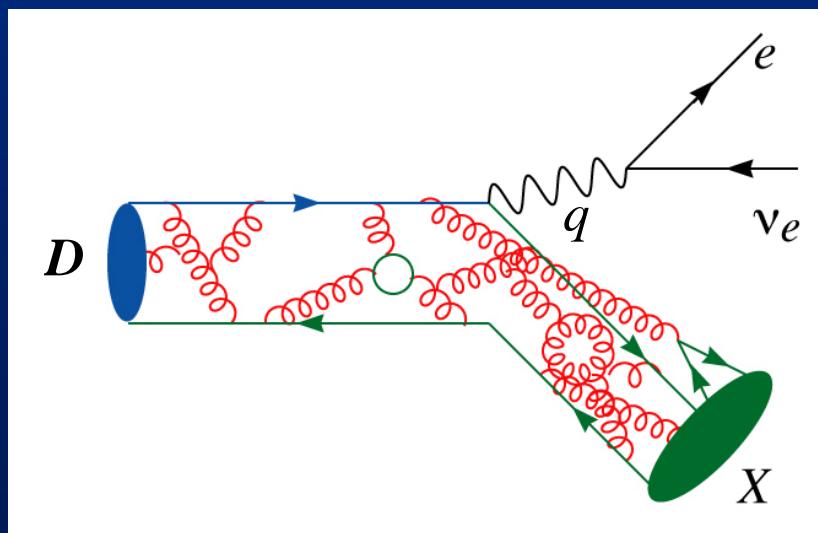
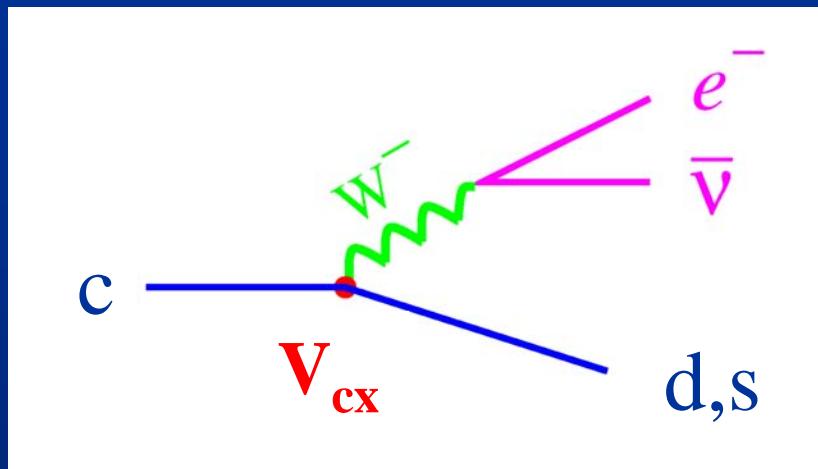
Calculations

- Comparable uncertainties already!

More data to come!



# Semileptonic Decays



Focus on recent results in  
Pseudoscalar final  
states:  $K, \pi$

Will not show:

- $D \rightarrow \eta e n / \eta' e n / \phi e n$  (J.Ge)  
presented in session B14
- $D \rightarrow V e \bar{\nu}$ ;  $V = K^*, \rho$

$$\frac{d\Gamma}{dq^2} = \frac{G_F^2}{24\pi^3} |V_{cx}|^2 p_X^3 |f_+(q^2)|^2$$

$$\begin{aligned} q^2 &= (p_D - p_X)^2 \\ &= M_D^2 + M_X^2 - 2E_X M_D + \vec{p}_D \cdot \vec{p}_X \end{aligned}$$

Fully reconstructed

$e^+ e^- \rightarrow D^{(*)} D^* X$  events

$\sqrt{s}=10.6$  GeV

Allows count of  $D^0$   
independent of decay

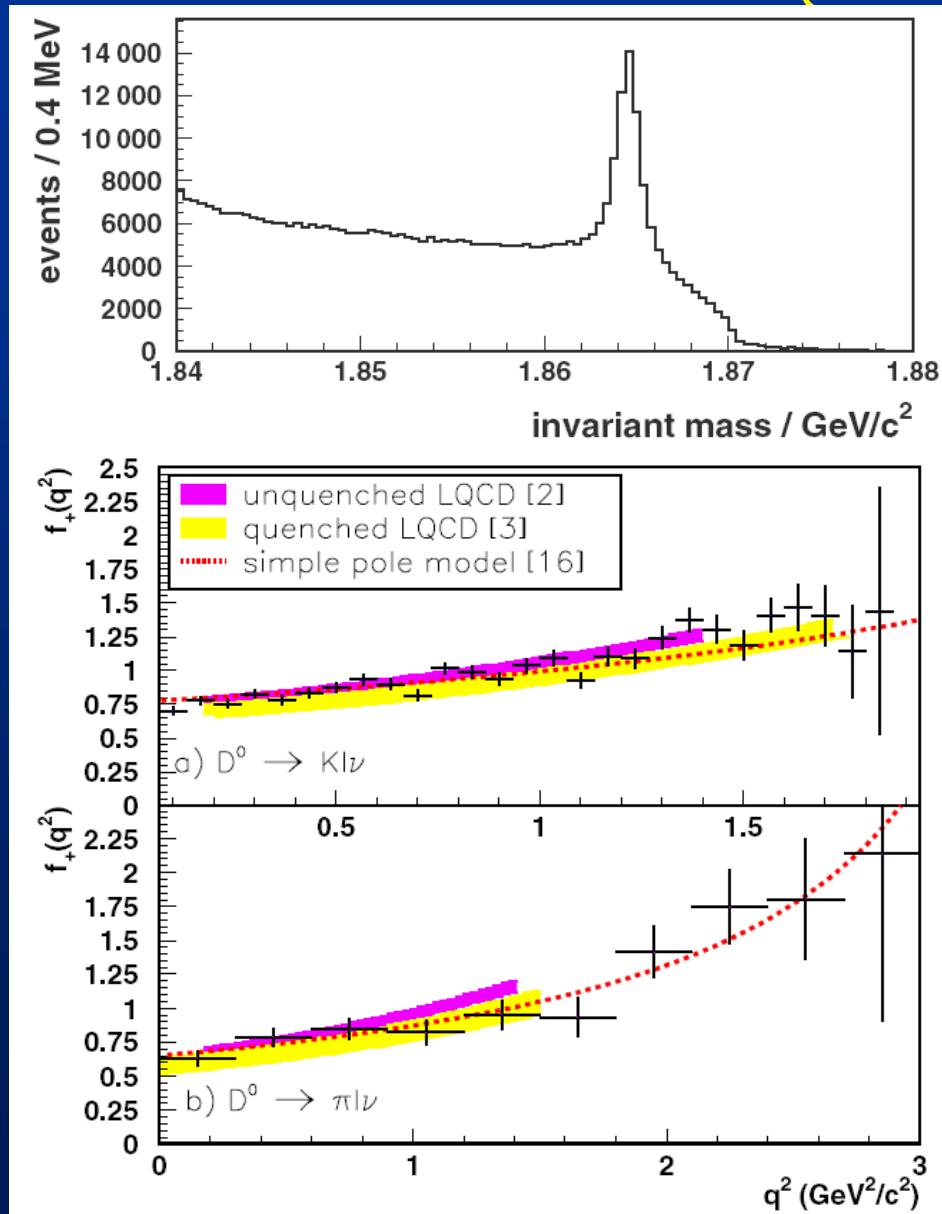
Neutrino inferred from  
missing  $E, p$

$D^{*+} \rightarrow D^0 \pi^+$  used to  
improve S/N

Excellent  $q^2$  resolution:  
 $\sigma(q^2)=0.017$  GeV $^2$

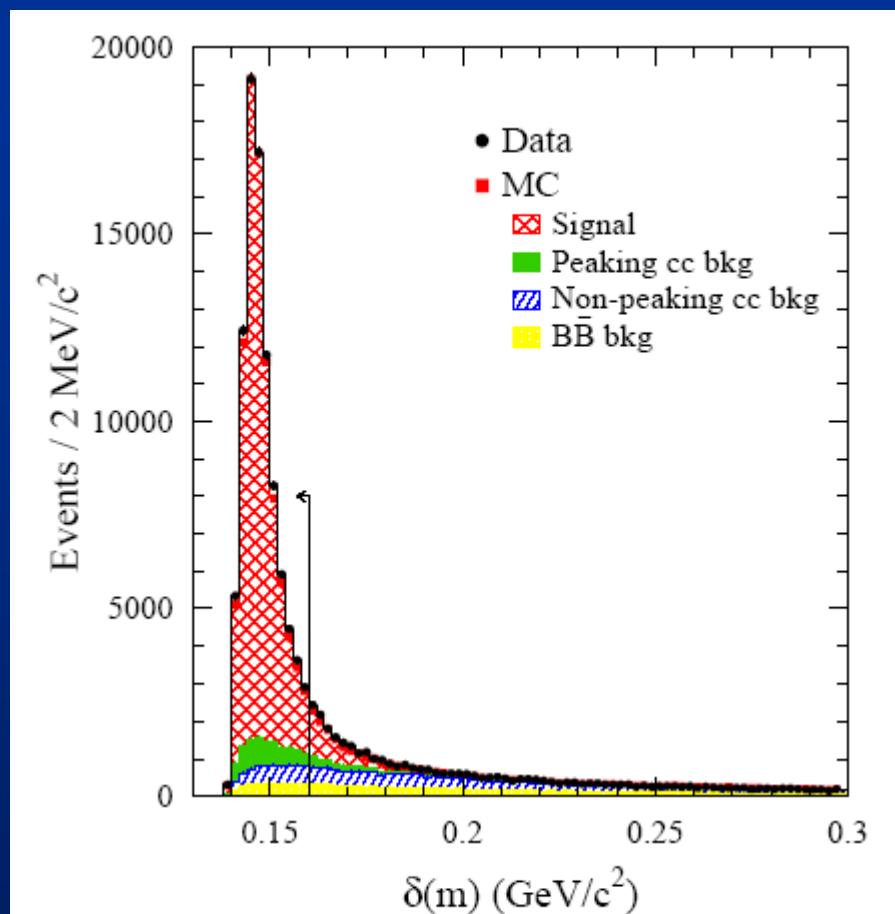
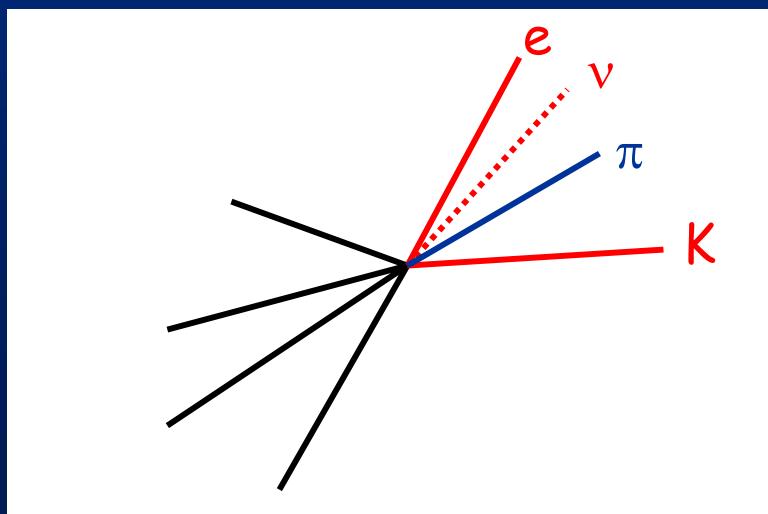
Measure rate directly

$$\frac{d\Gamma}{dq^2} = \frac{G_F^2}{24\pi^3} |V_{cx}|^2 p_X^3 |f_+(q^2)|^2$$



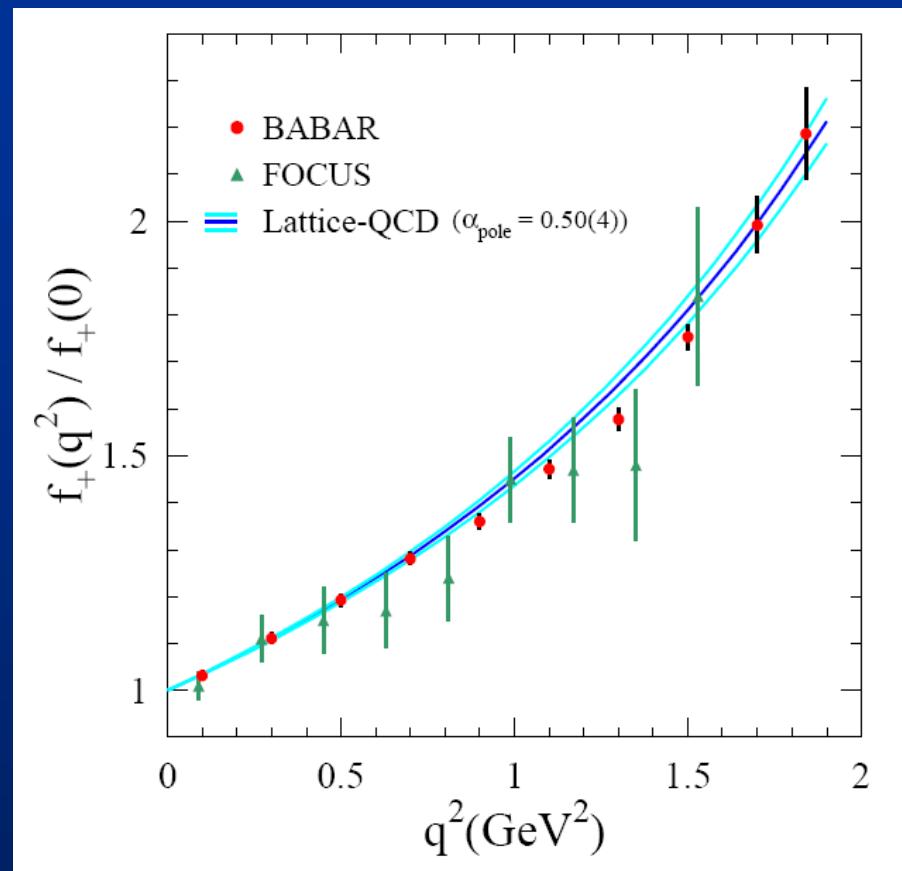
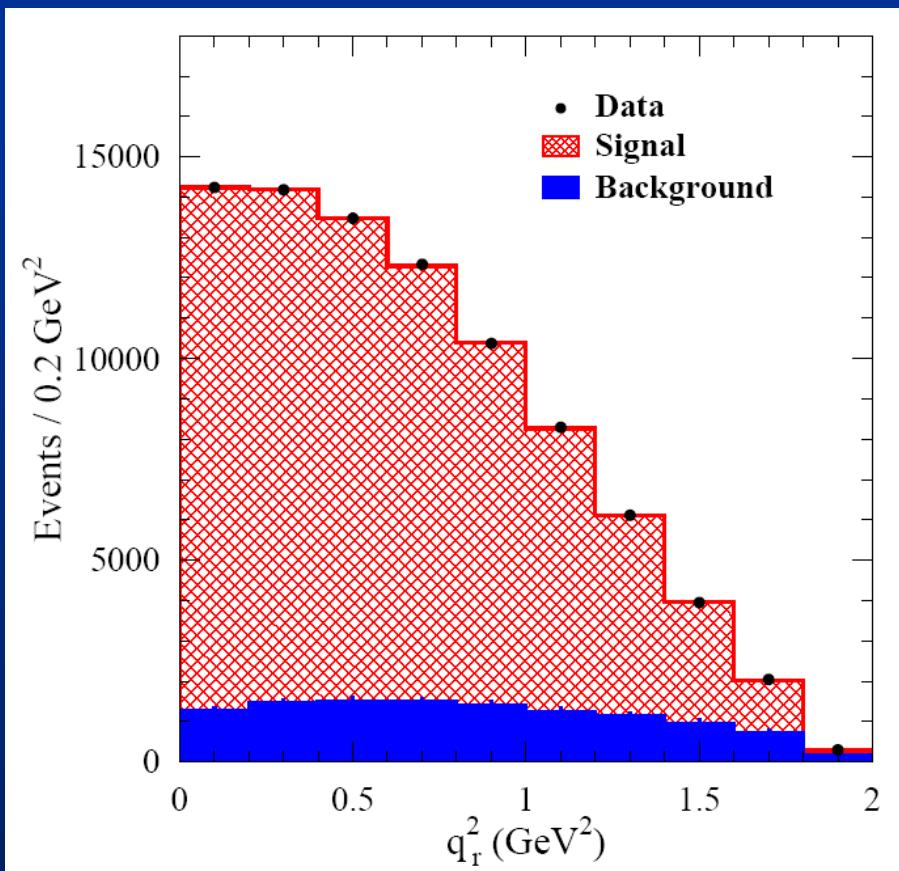
$e^+e^- \rightarrow c\bar{c}$  at  $\sqrt{s}=10.6 \text{ GeV}$

- Reconstruct  $D^{*+} \rightarrow \pi^+ D^0$  and signal  $D^0 \rightarrow K e \nu$
- Estimate  $p_D$  and  $E_\nu$  with remaining event & kinematic fits
- Use Neural Nets to suppress backgrounds



$$\delta m = M(D^*) - M(D)$$

- high statistics
- good S/N



$$q^2 = (p_D - p_X)^2$$

85k signal/11k background

- Corrected spectrum compared to LQCD<sup>1</sup>, FOCUS<sup>2</sup>

<sup>1</sup> Aubin et al. PRL 94, 011601 (2005)

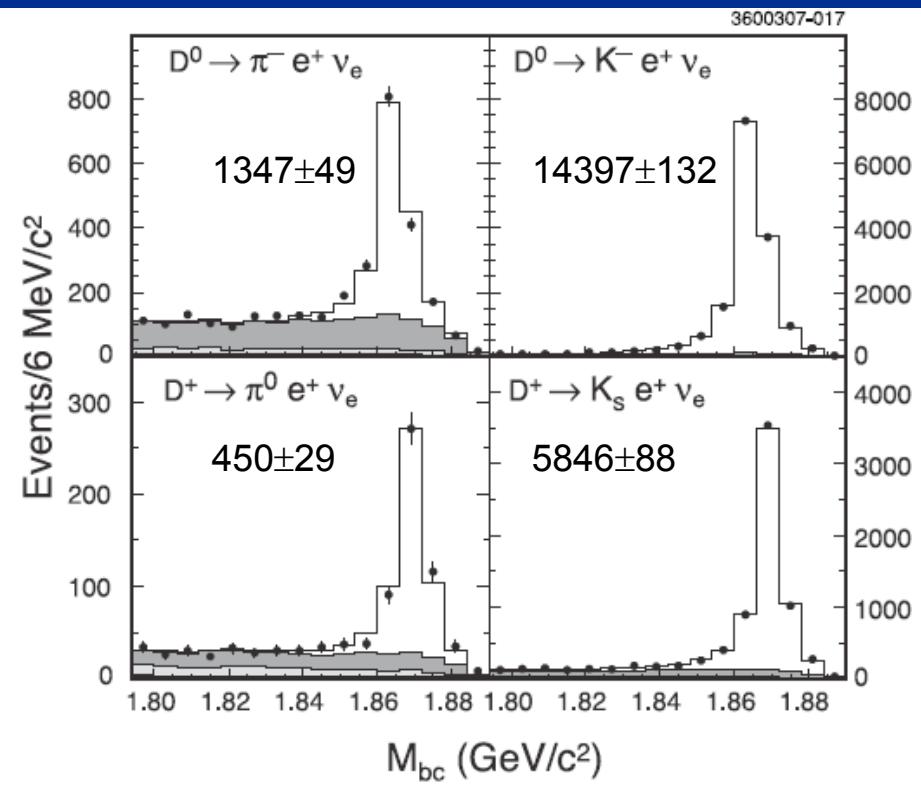
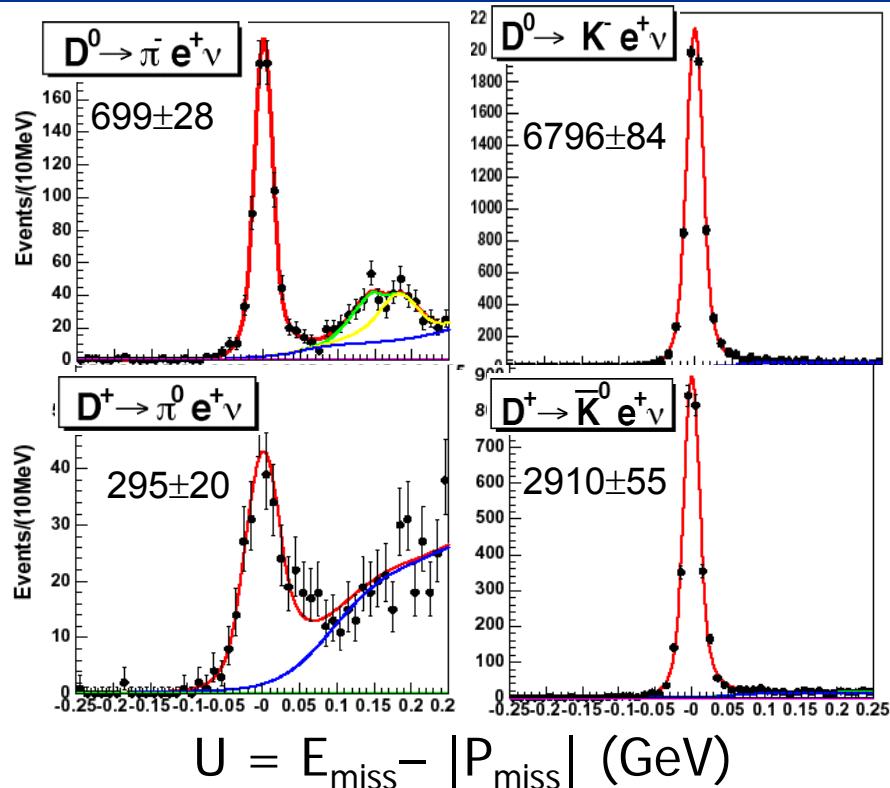
<sup>2</sup> PLB607, 233 (2005)

CLEO-c  $D \rightarrow \pi e^+ \nu$  &  $D \rightarrow K e^+ \nu$ Tagged Analysis

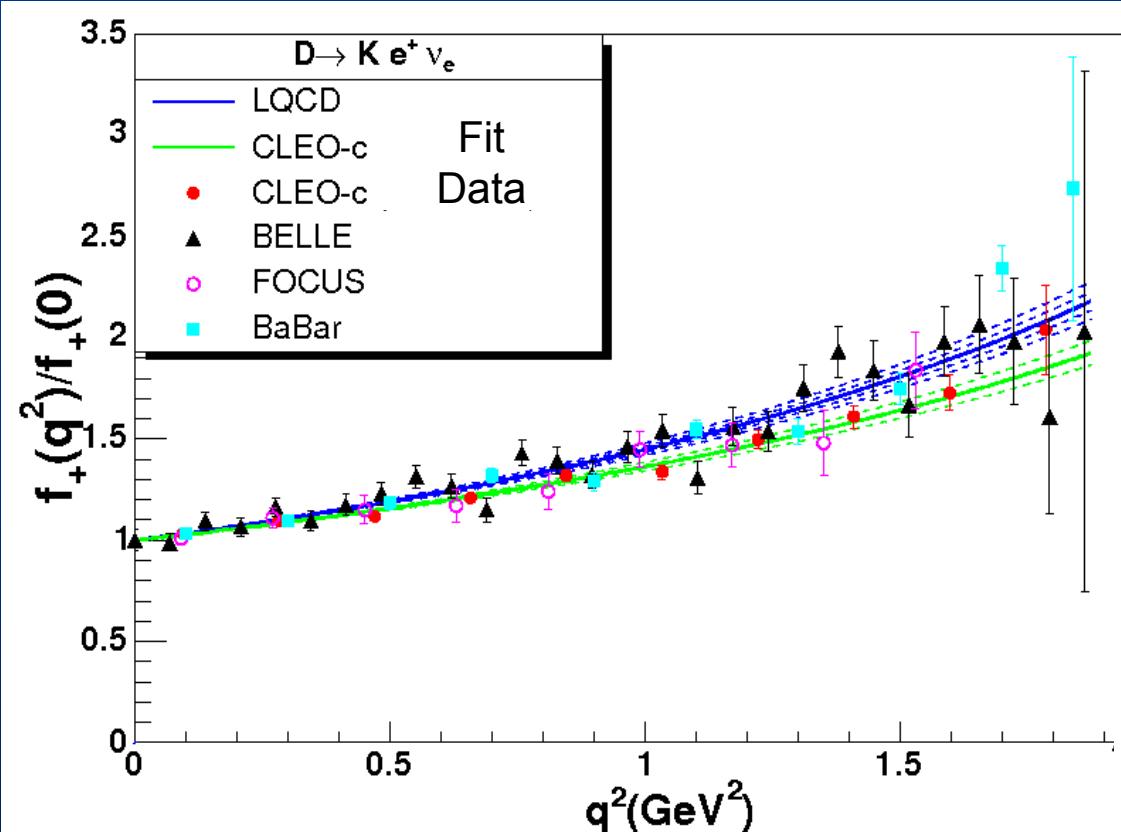
Preliminary

281 pb<sup>-1</sup>

Presented by B.Xin Session B14

Neutrino Reconstruction

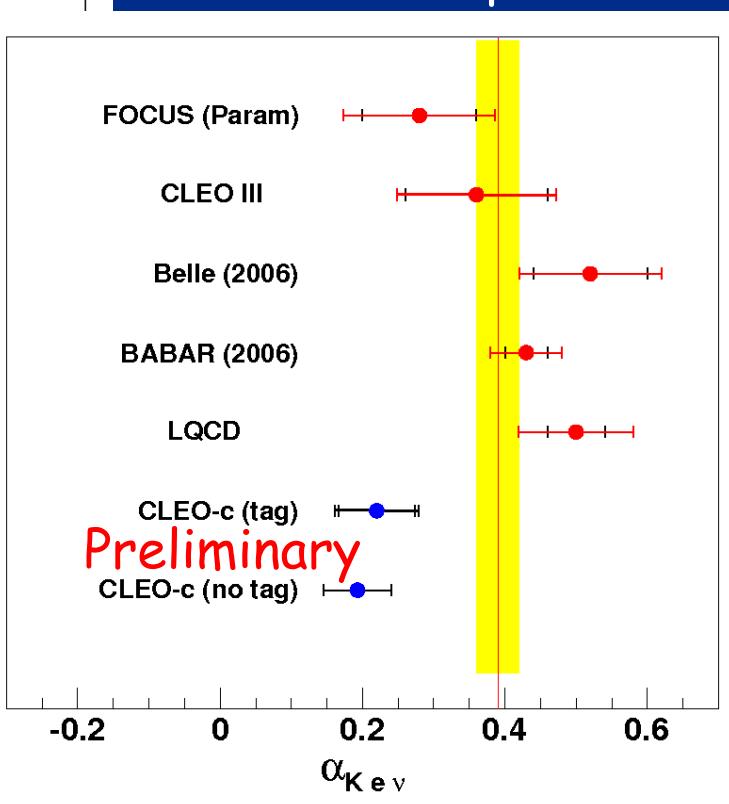
- extremely clean
- well separated backgrounds
- $q^2$  resolution:  $\sigma=0.012 \text{ GeV}^2$
- better statistics
- larger systematic uncertainty
- ~40% overlap in event samples

$D^0 \rightarrow K^- e^+ \nu_e$  Form Factor Comparisons

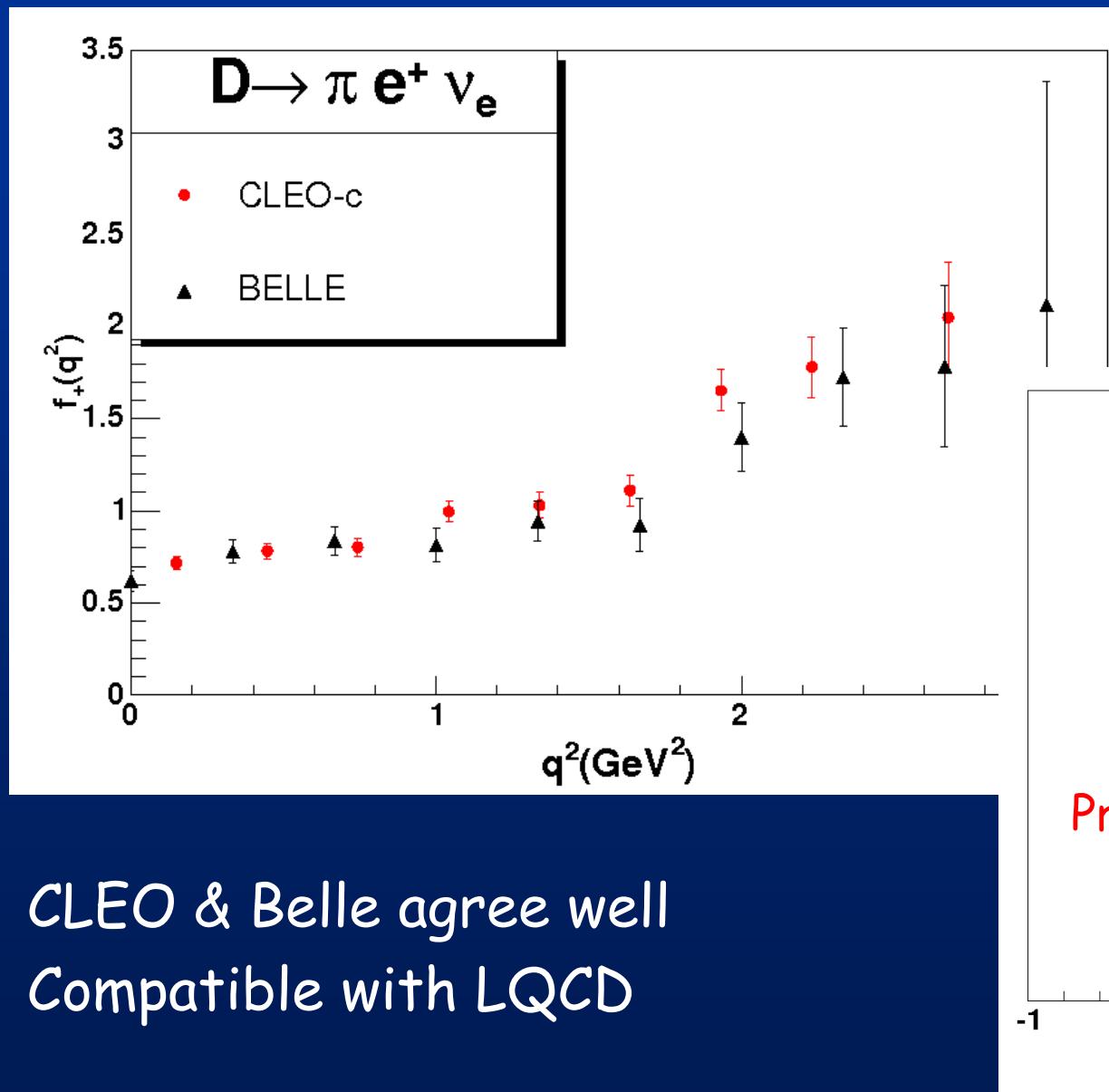
LQCD: Aubin et al. PRL 94 011601 (2005)

High statistics test of shape  
CLEO prefers smaller slope  $\alpha$

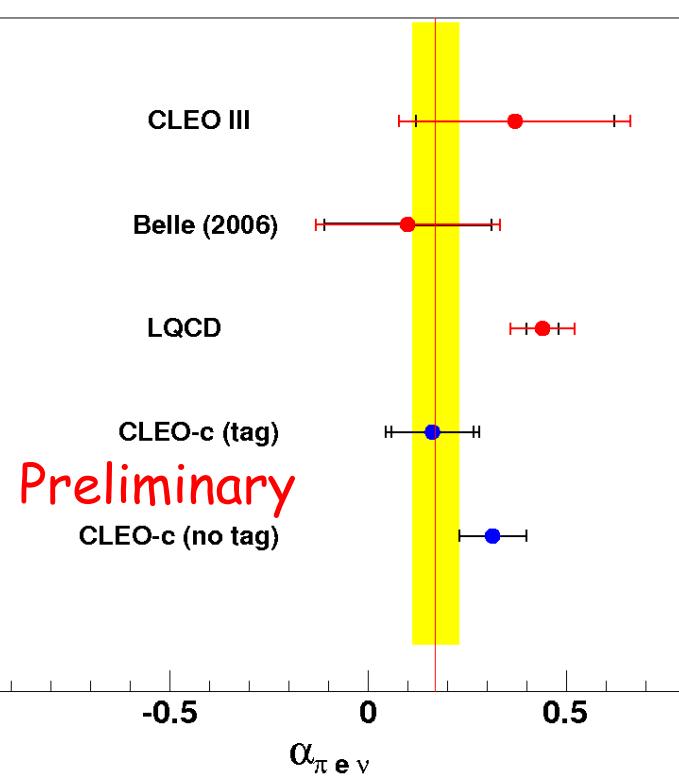
Single parameter fit  
“modified pole”



# $D^0 \rightarrow \pi^- e^+ \nu_e$ Form Factor Comparisons



CLEO & Belle agree well  
Compatible with LQCD

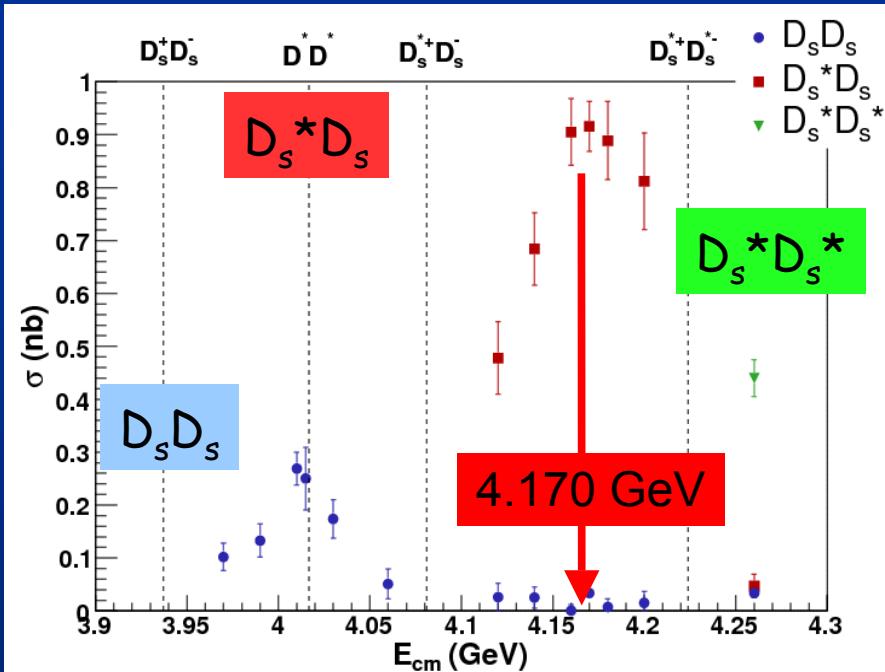


# Summary & Conclusions

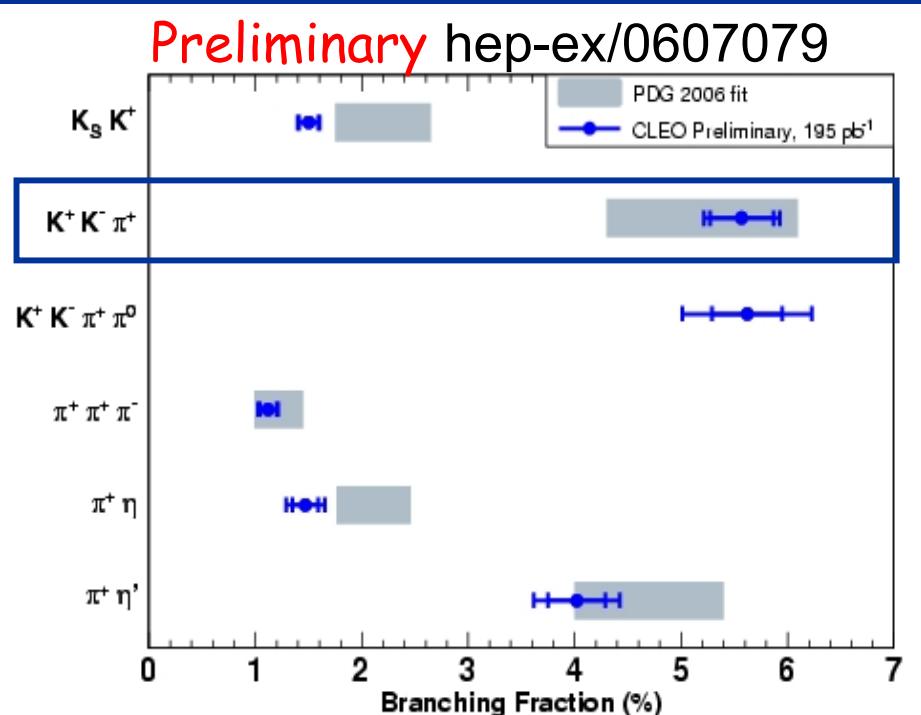
- Charm decays are measured with precision
- Charm measurements complement flavor physics investigations in the b sector
  - aid interpretation of B mixing
  - assist extraction of  $V_{CKM}$  especially  $V_{ub}$
  - by constraining QCD effects
- Unquenched Lattice QCD decay constant results appear trustworthy but...
  - experimental precision exceeds current LQCD
  - hints of differences for semileptonic Form factors
    - Kev experimental discrepancy?
  - normalization of form factor  $\rightarrow$  10% uncertainty on  $V_{cx}$
- Additional data from BaBar, Belle, CLEO
  - more precise results to come!

# Additional Slides

# CLEO-c $D_s$ Hadronic results



- Tagging with  $D_s D_s^*$
- $D_s^* \rightarrow D_s \gamma$



Partial BF for  $D_s \rightarrow \phi \pi$   
interference with  $f_0(980)$

$$M(KK) = M_\phi \pm 10 \text{ MeV}$$

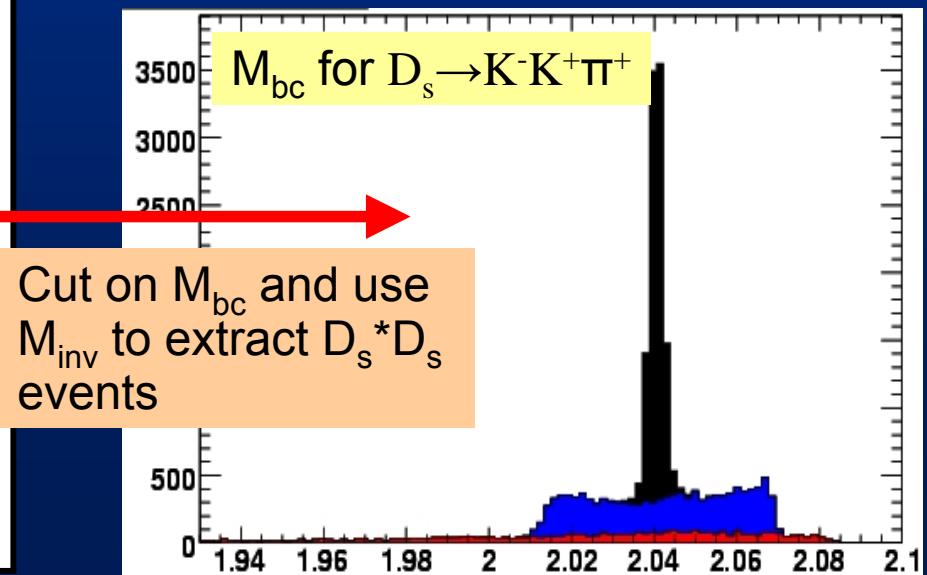
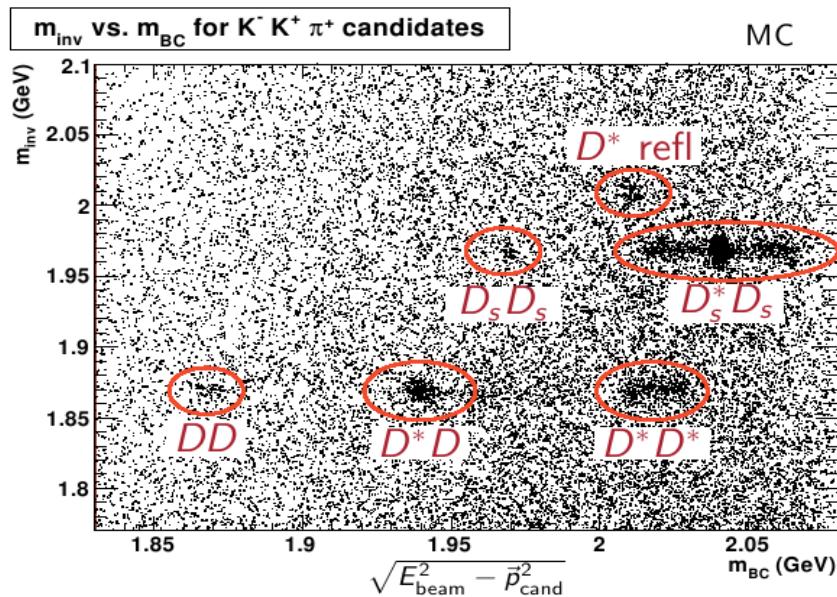
$$BF = (1.98 \pm 0.12 \pm 0.09)\%$$

$$M(KK) = M_\phi \pm 20 \text{ MeV}$$

$$BF = (2.25 \pm 0.13 \pm 0.12)\%$$

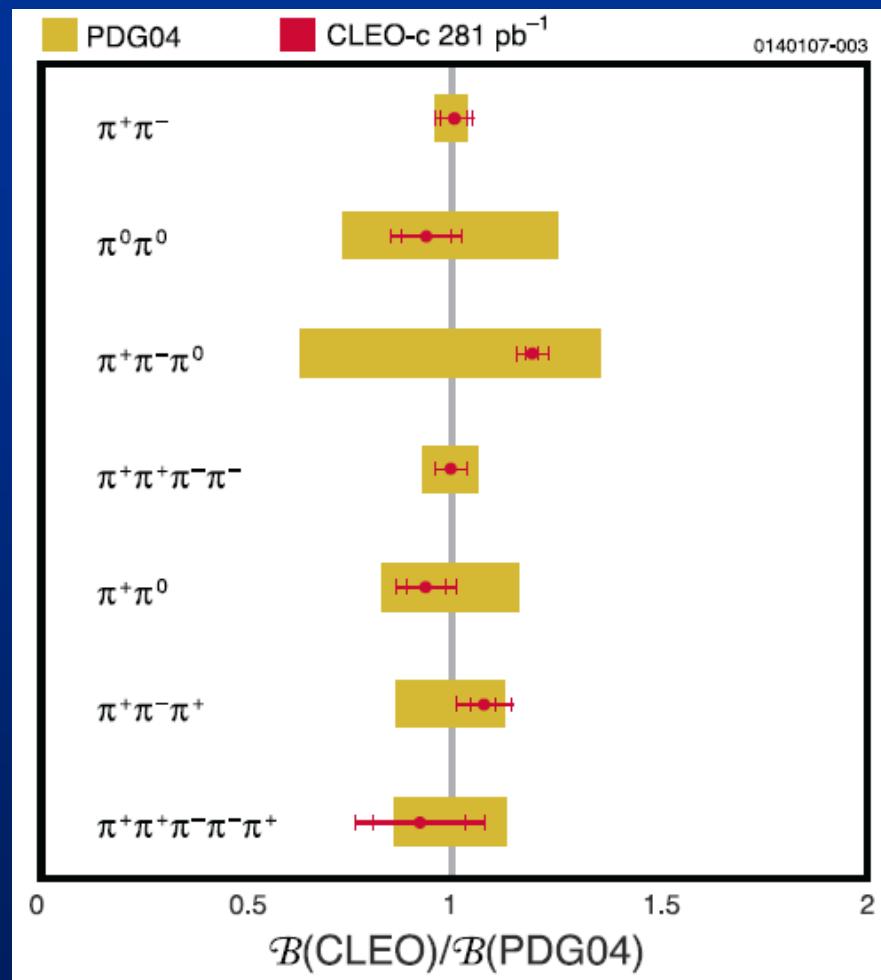
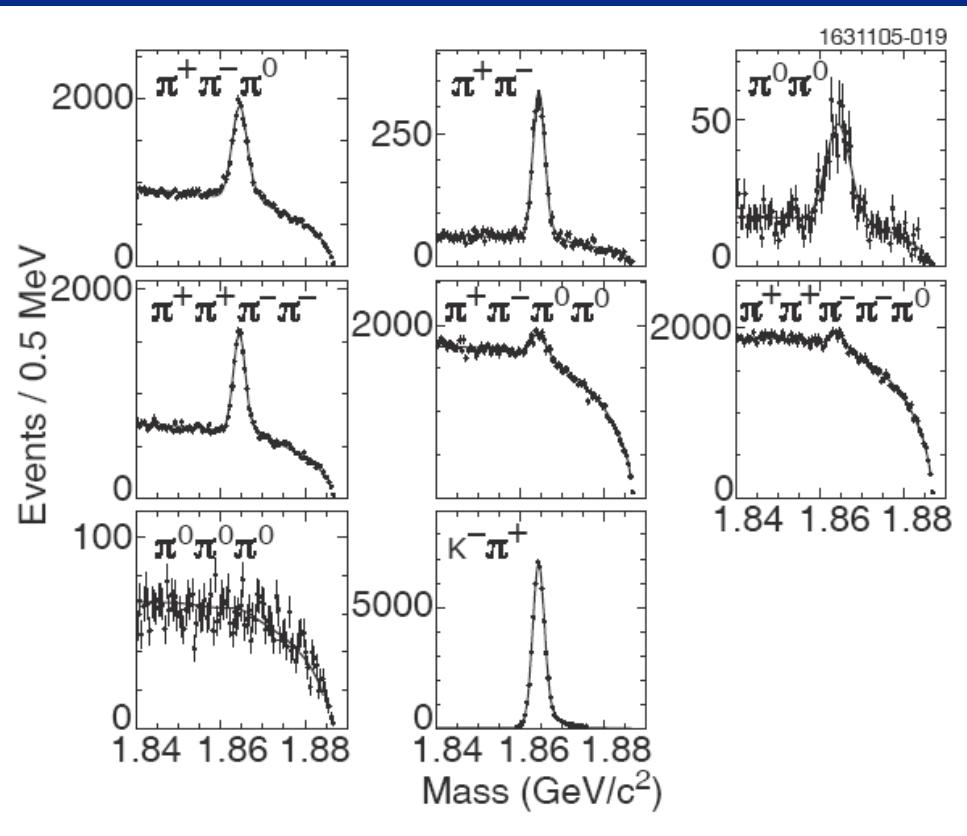
# CLEO-c $D_s$ Hadronic Decays

$M_{inv}$  vs.  $M_{bc}$  for  $K^-K^+\pi^+$  candidates in MC



# Additional Hadronic Decays

- Additional modes from CLEO-c
  - PRL 96, 081802 (2006)
  - Single Tag Measurement



D<sup>0</sup> modes shown on left